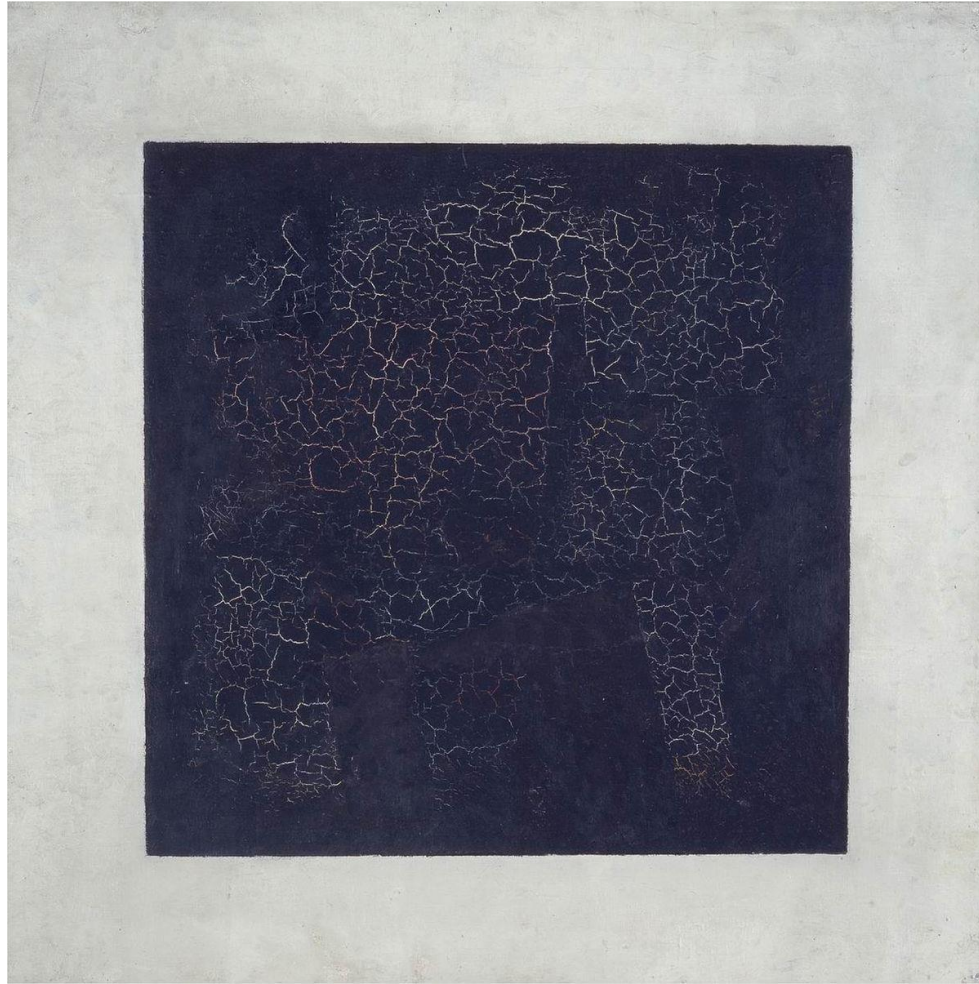


Why do people like abstract art?

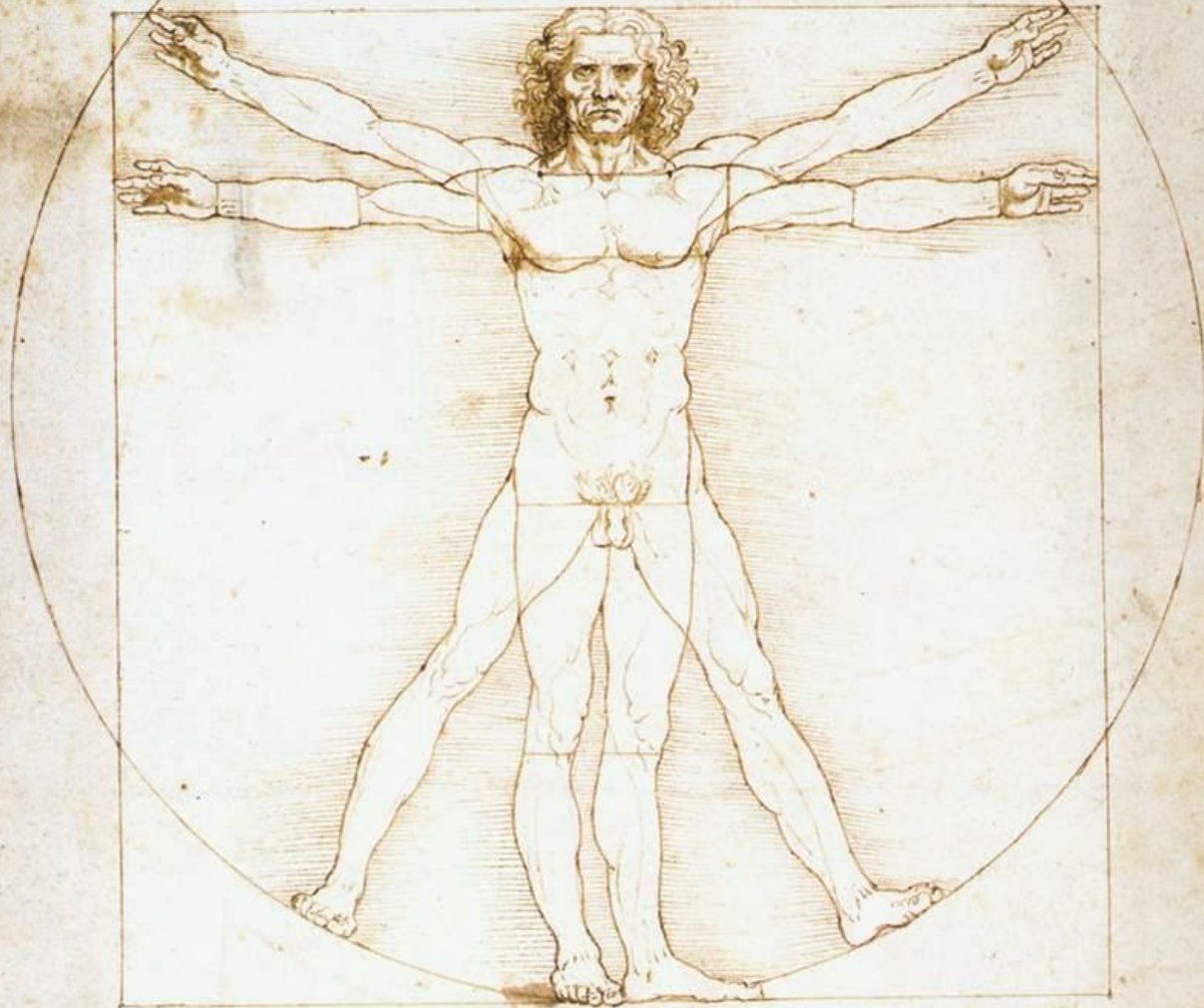


Frank Thuijsman

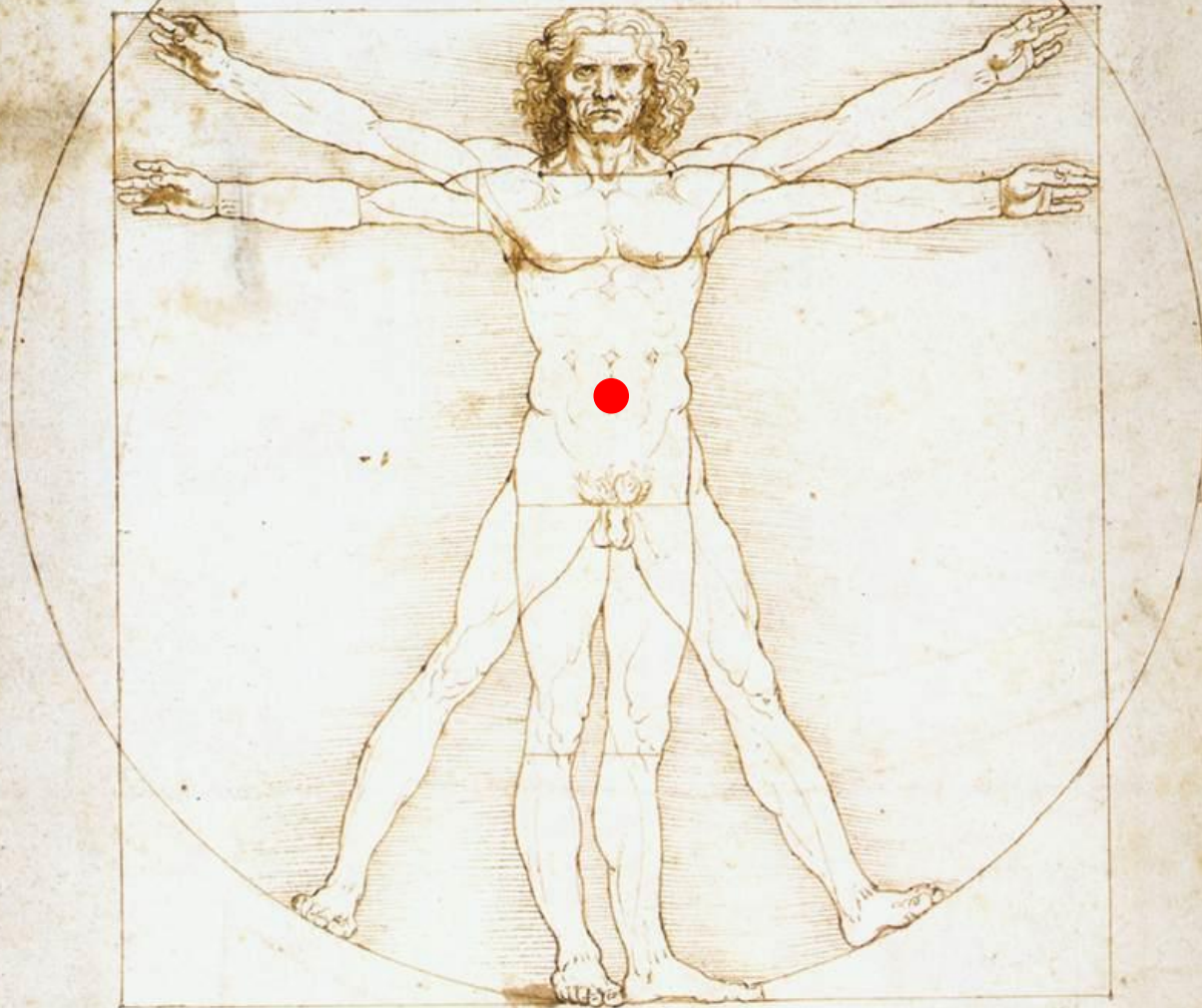
Kazimir Malevich (1915): The Black Square



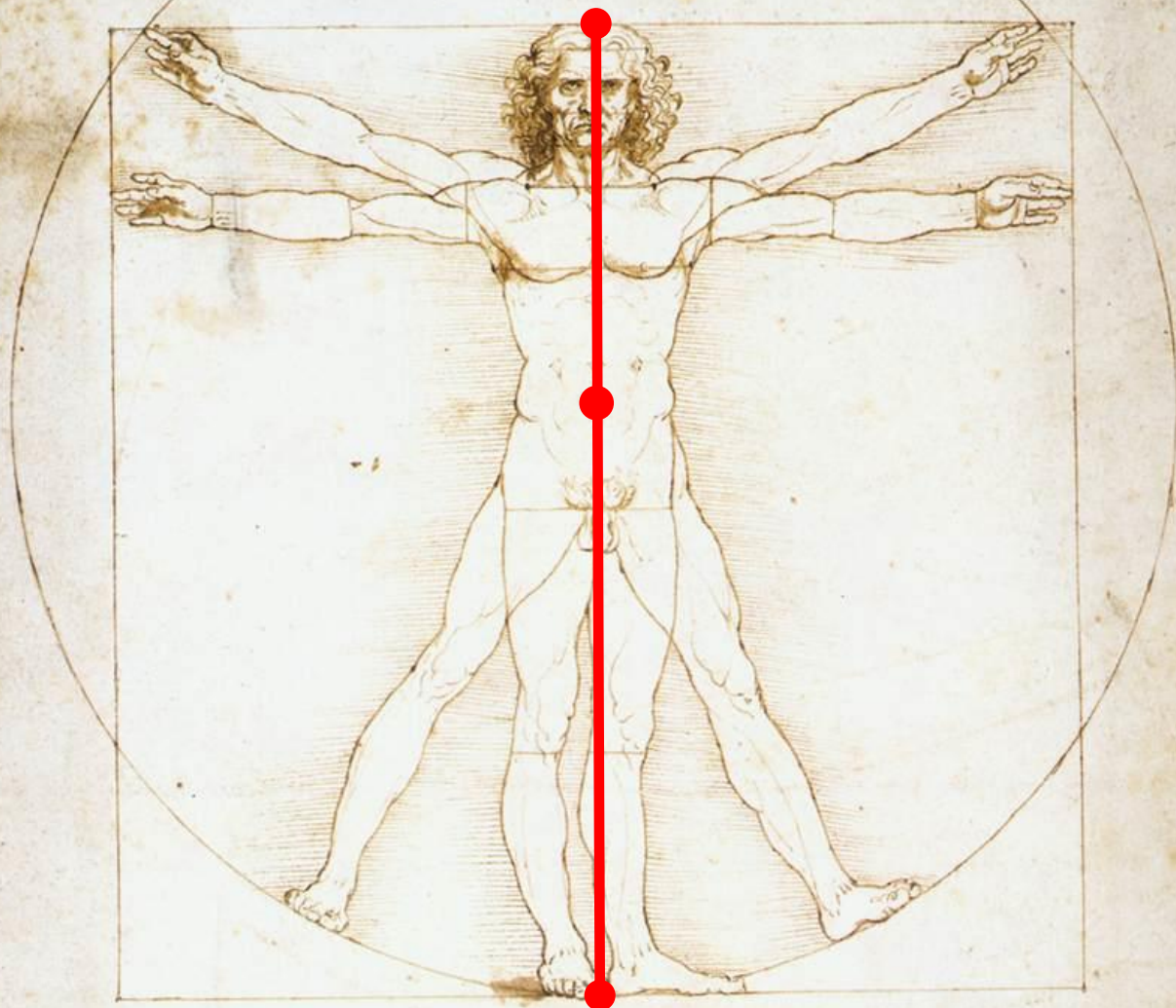
Da Vinci – Vitruvius (1485/1490)



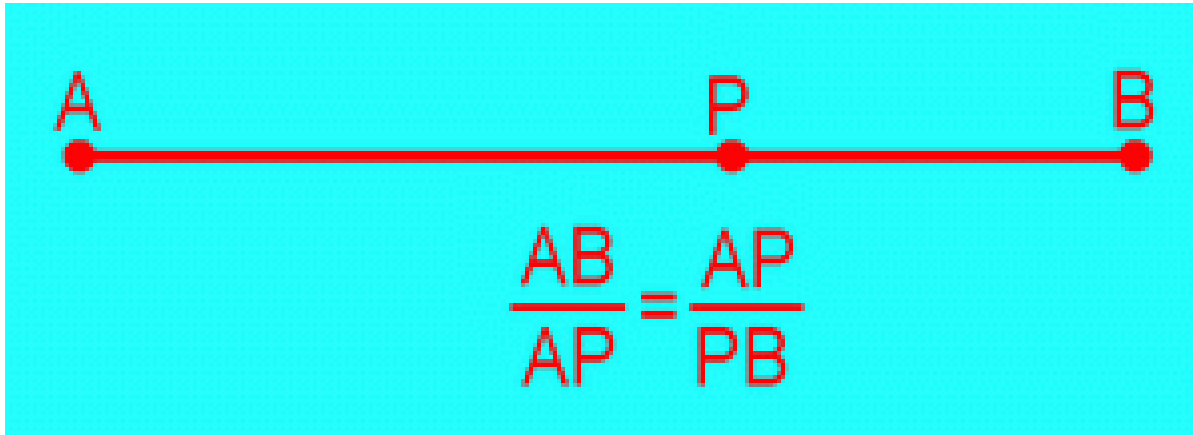
Da Vinci – Vitruvius (1485/1490)



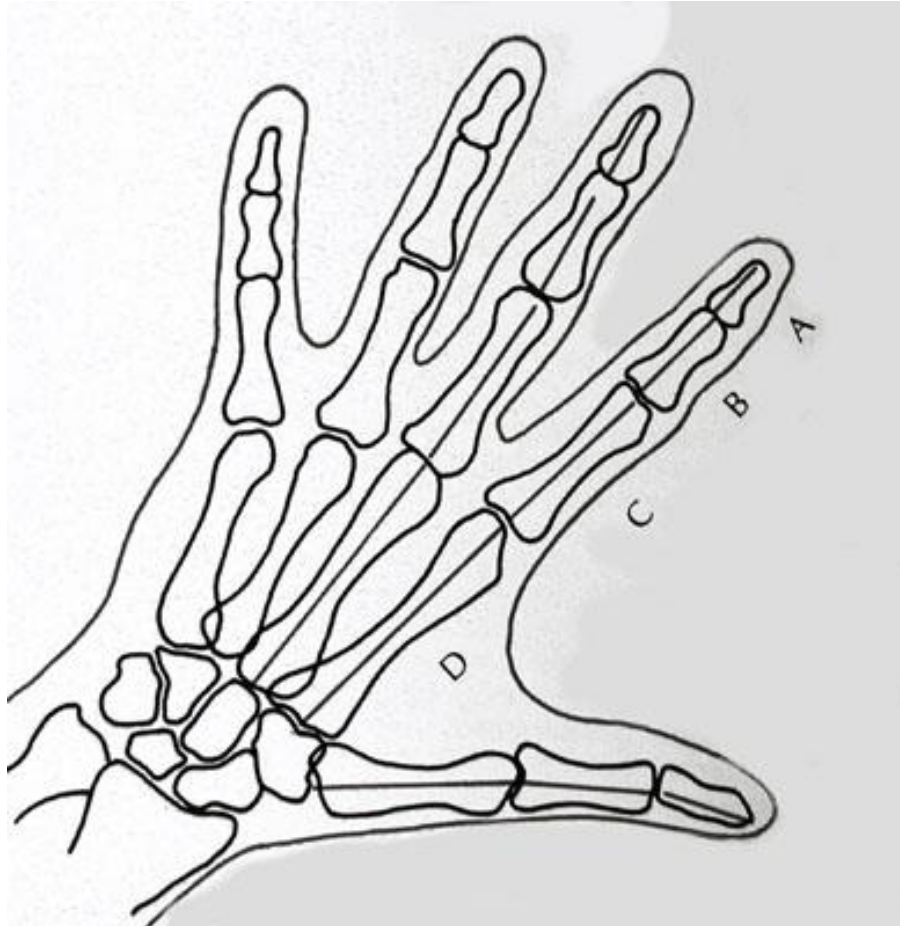
Da Vinci – Vitruvius (1485/1490)



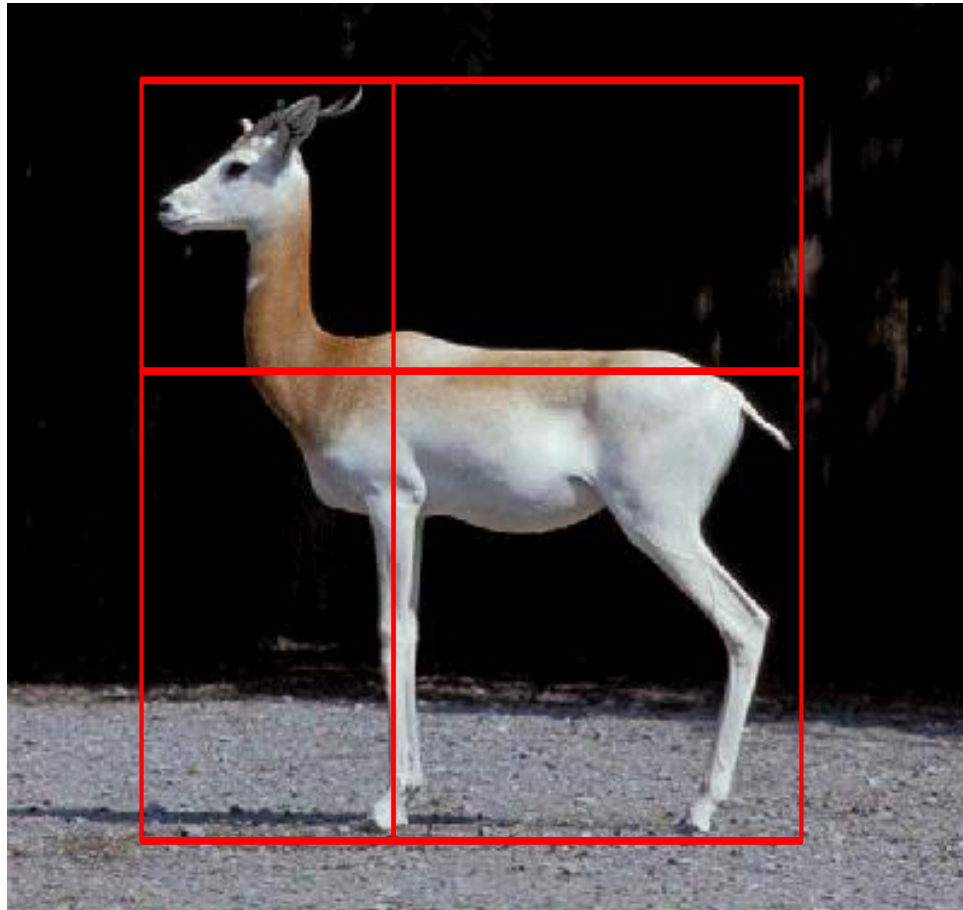
Golden Ratio



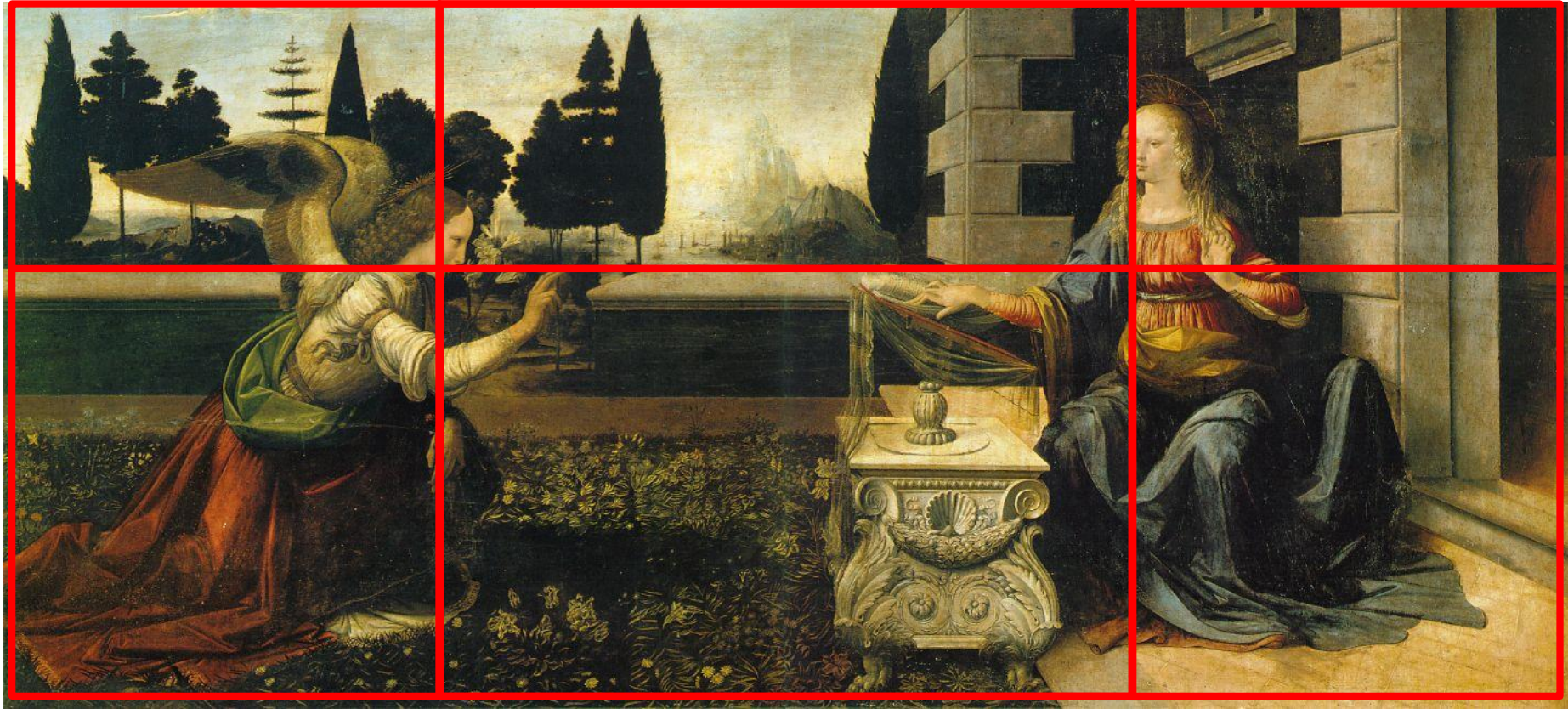
Golden Ratio



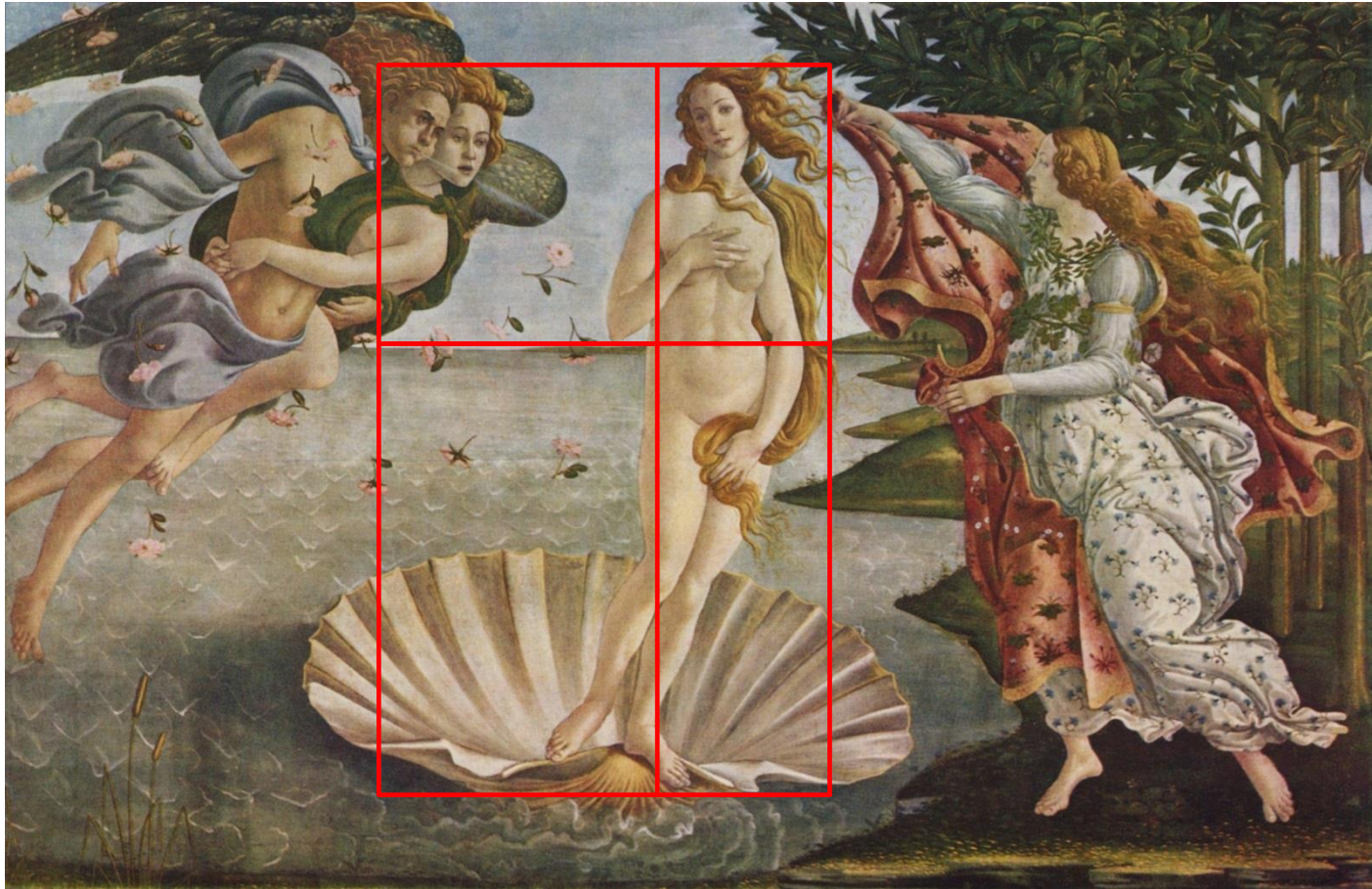
Golden Ratio



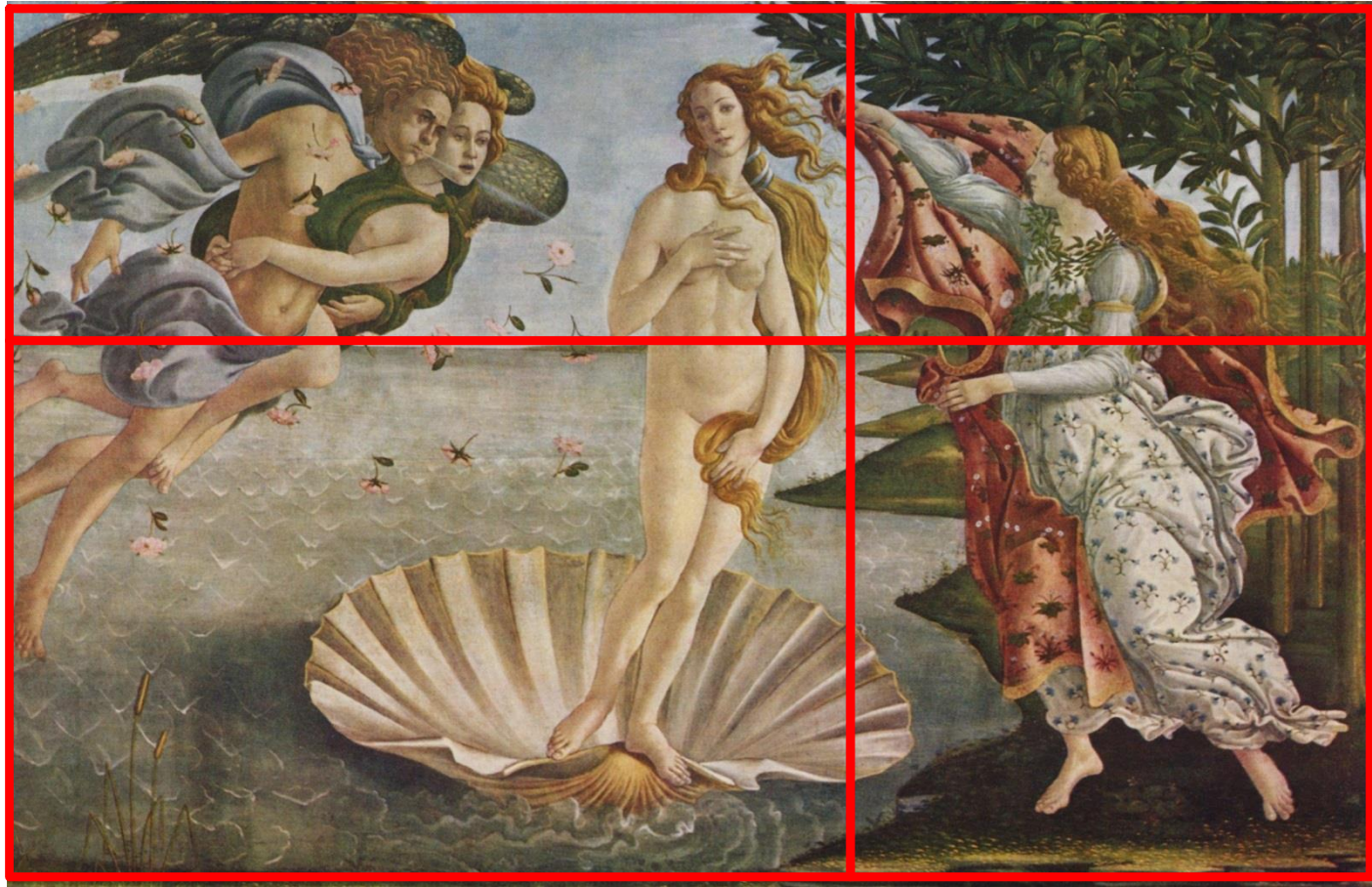
Golden Ratio – Da Vinci (1475)



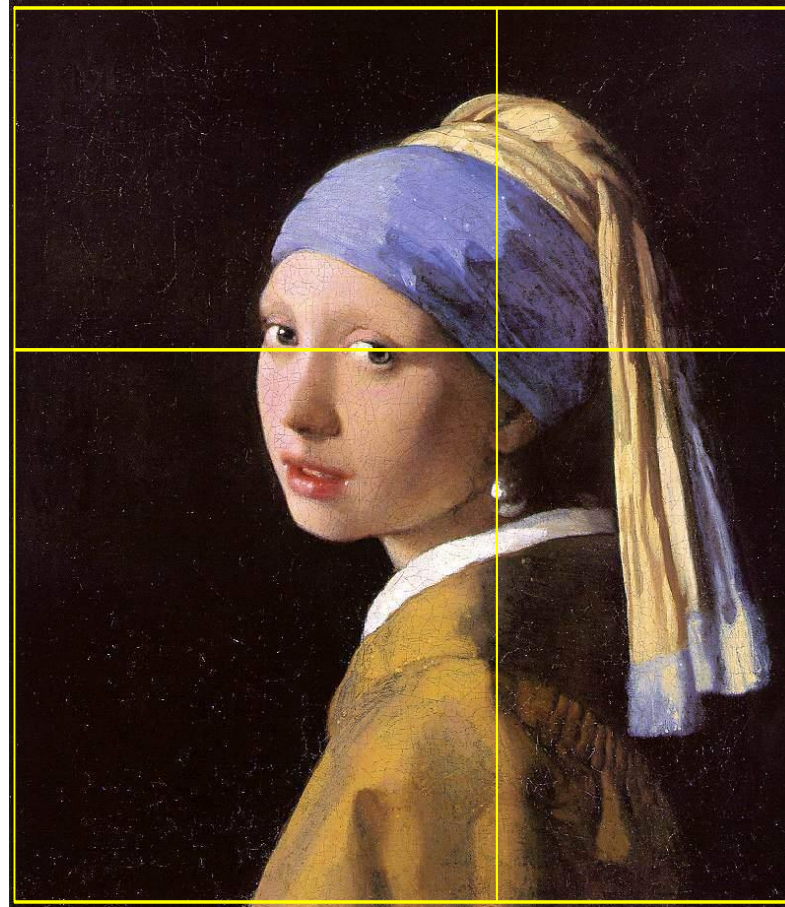
Golden Ratio – Botticelli (1485)



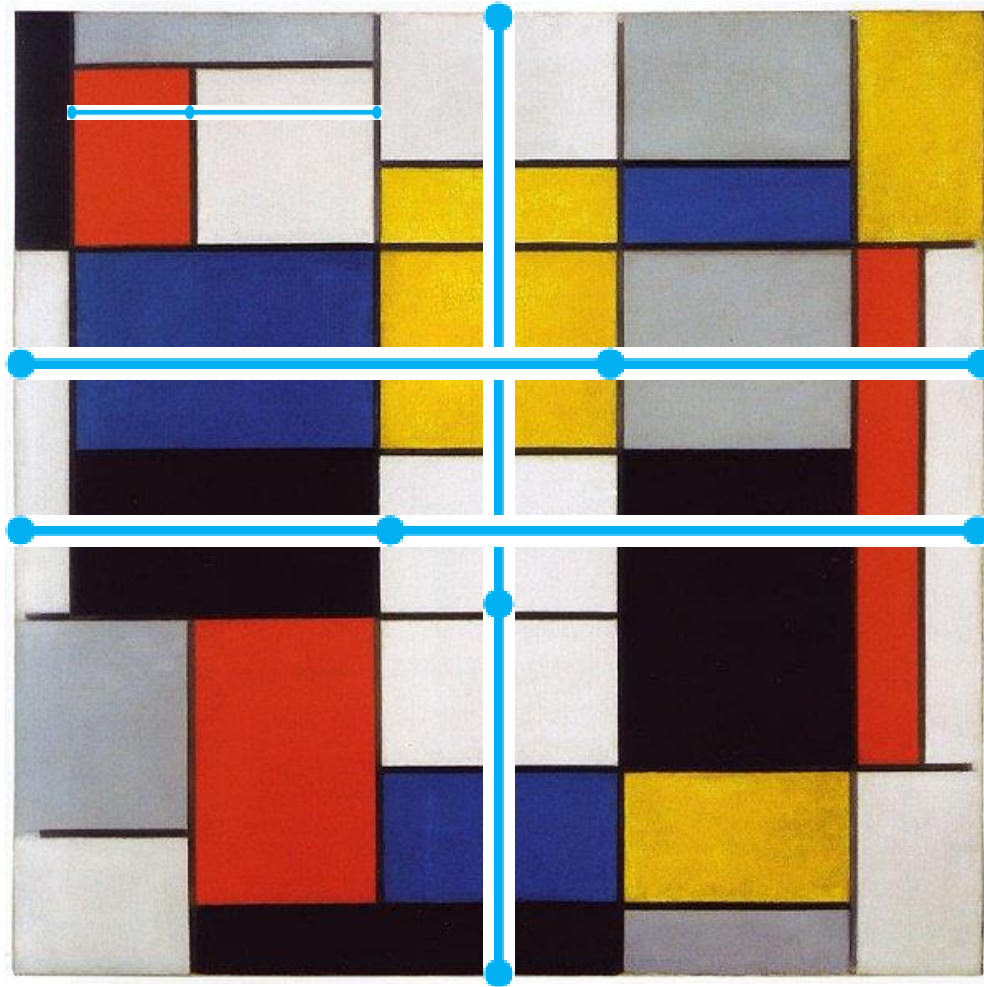
Golden Ratio – Botticelli (1485)



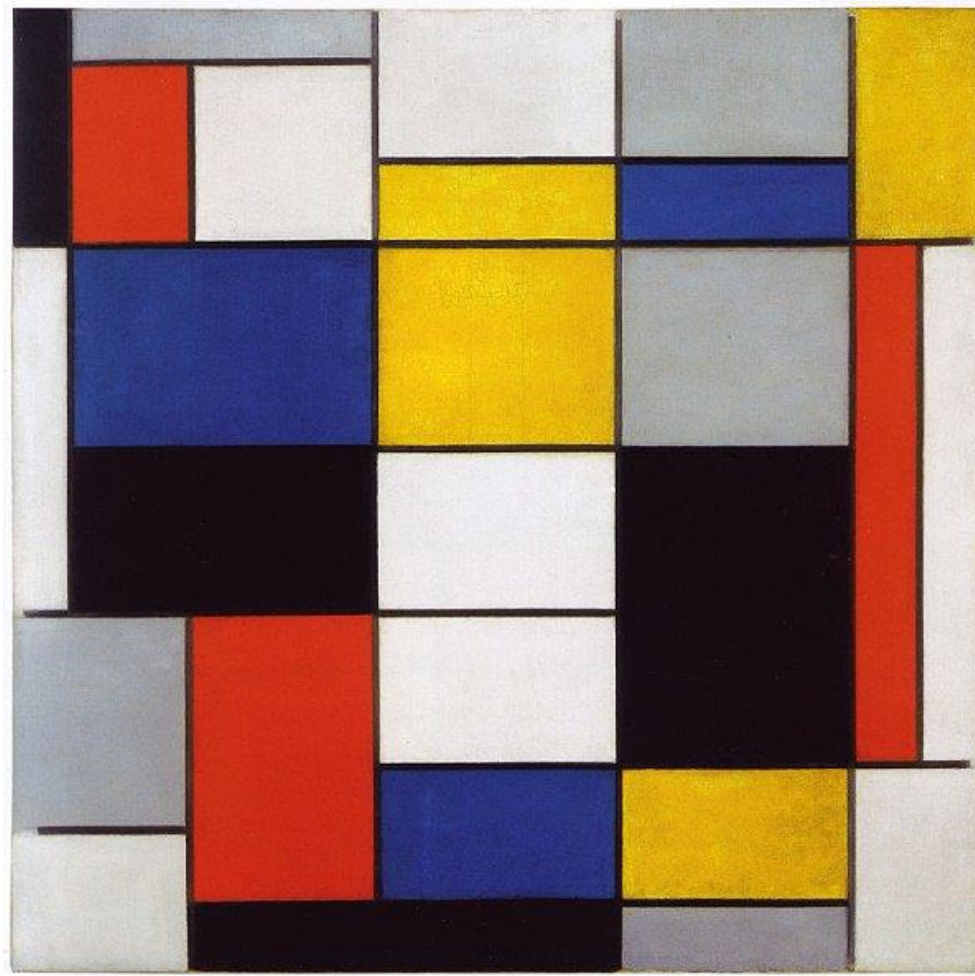
Golden Ratio – Vermeer (1665)



Golden Ratio – Mondriaan (1920)



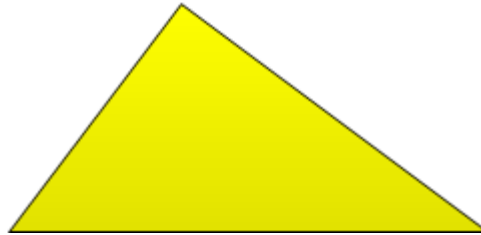
Piet Mondriaan (1920): Composition A



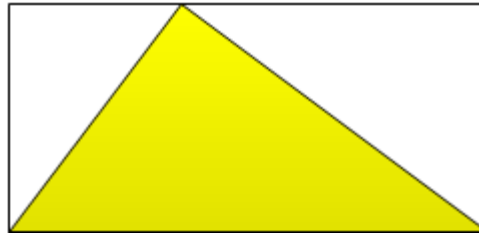
Marie van Vollenhoven: The Sky is the Limit



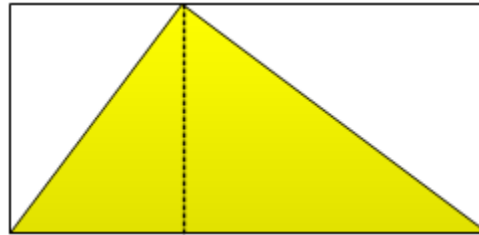
Beyond the Sky



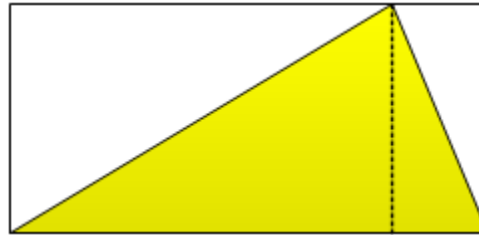
Beyond the Sky



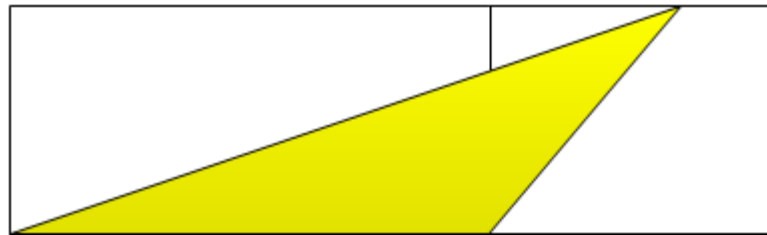
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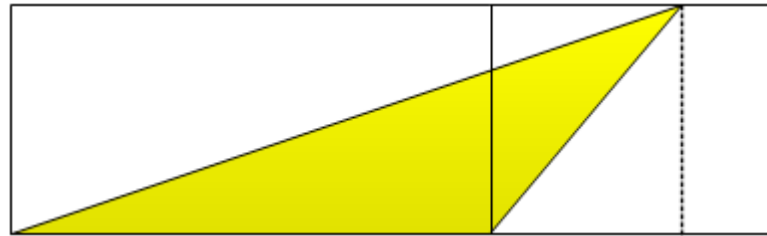
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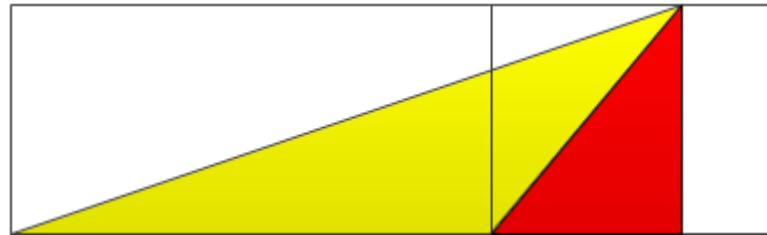
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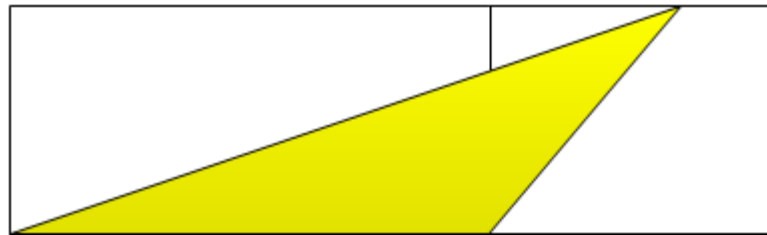
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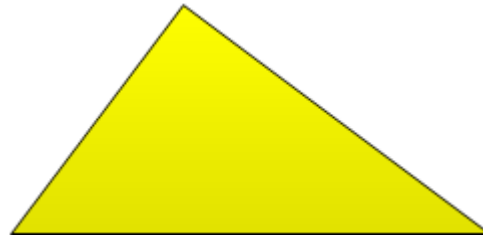
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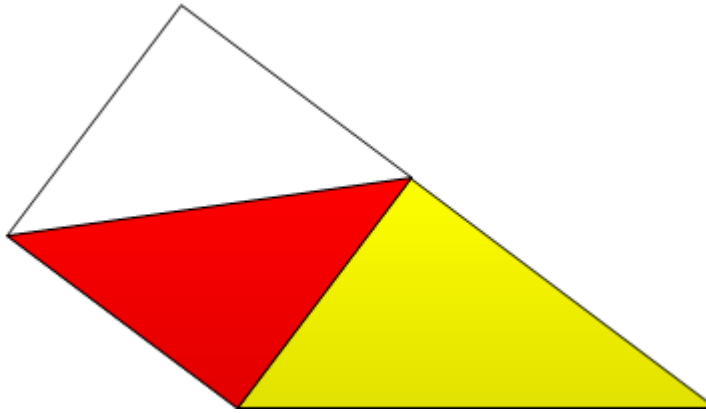
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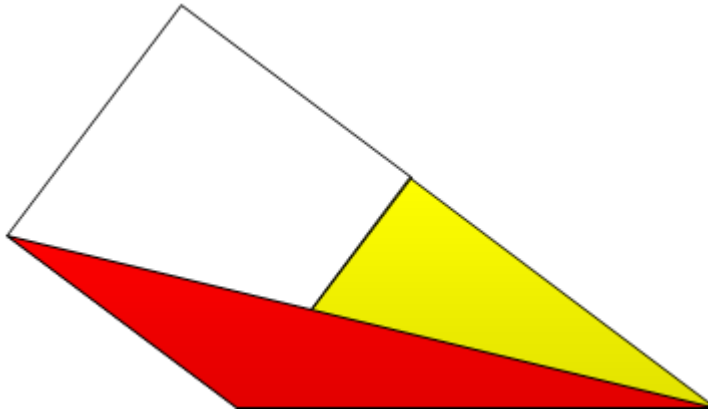
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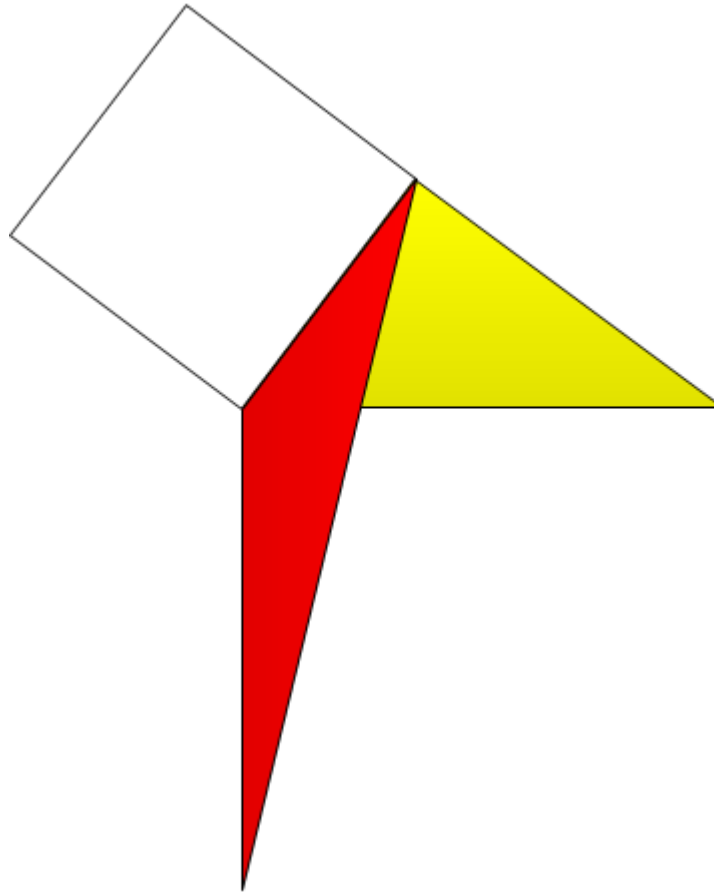
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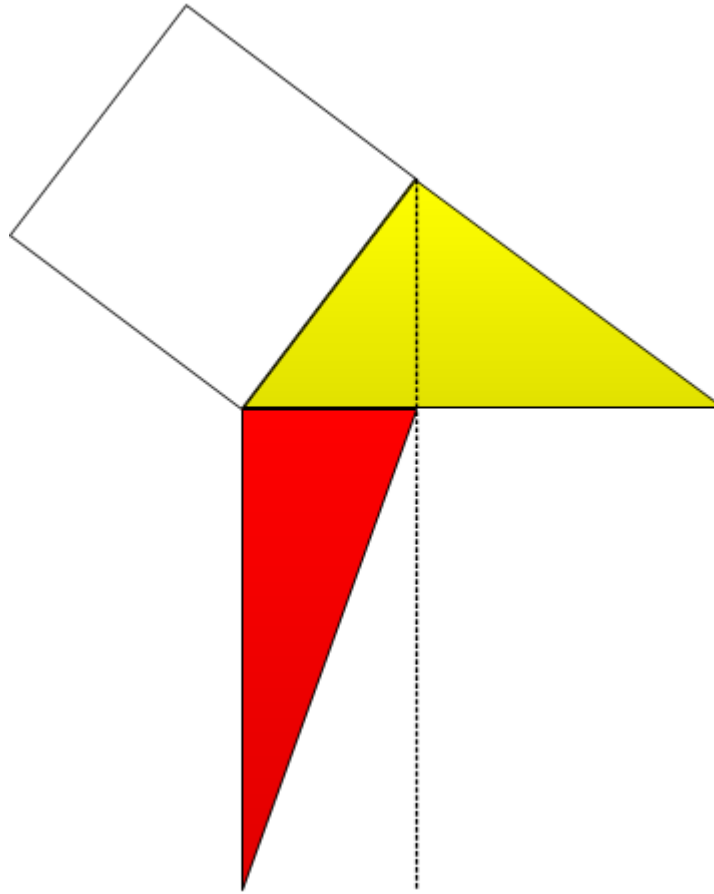
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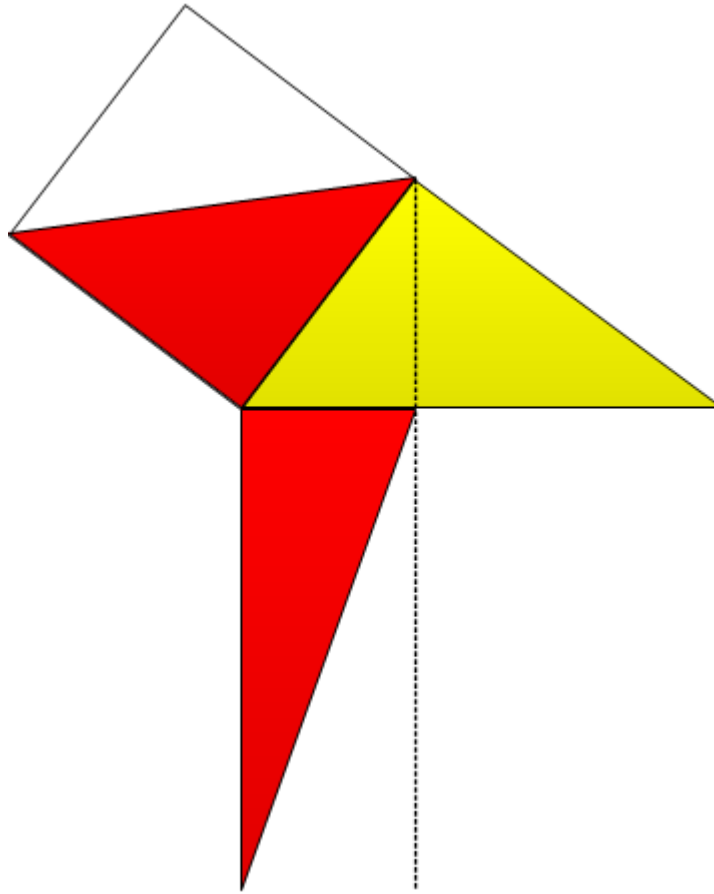
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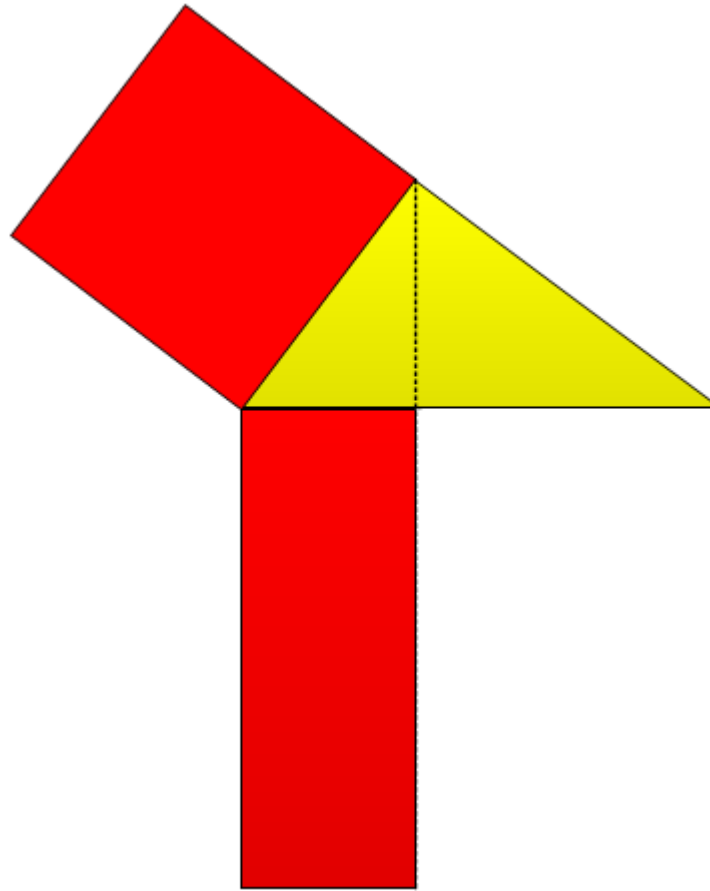
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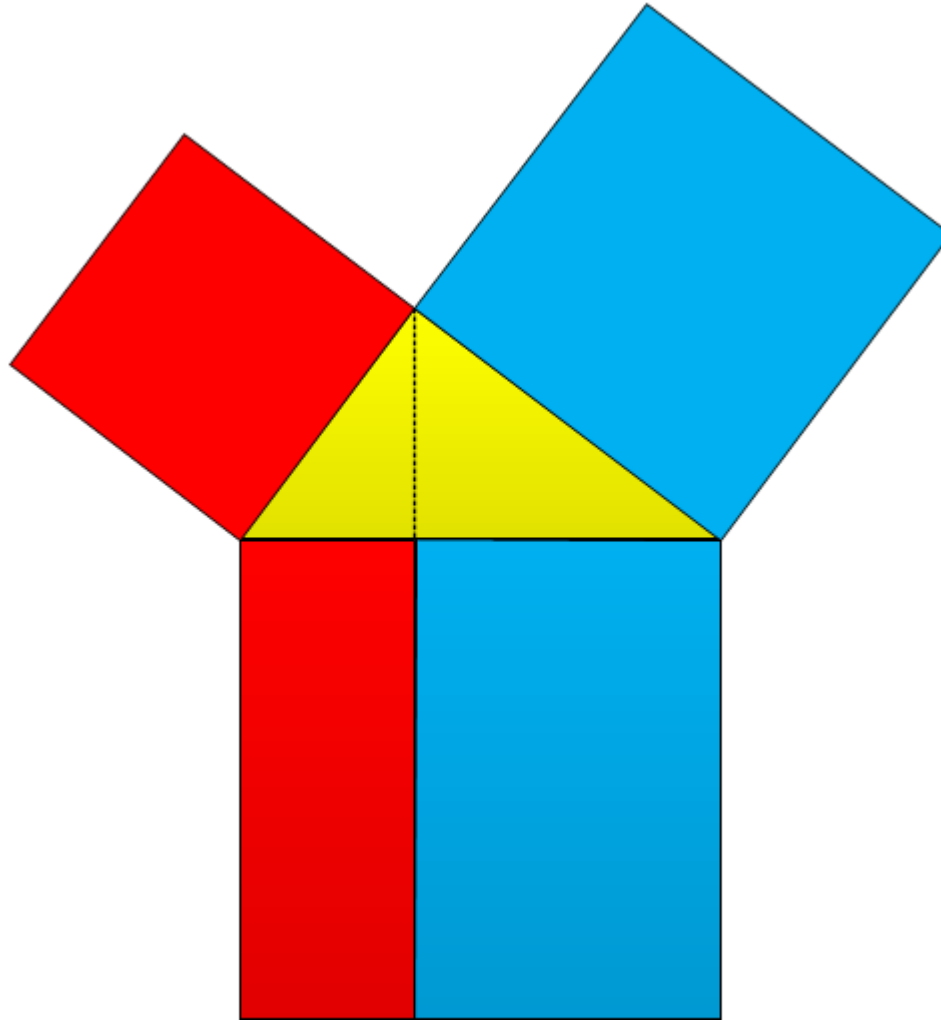
Beyond the Sky



Beyond the Sky

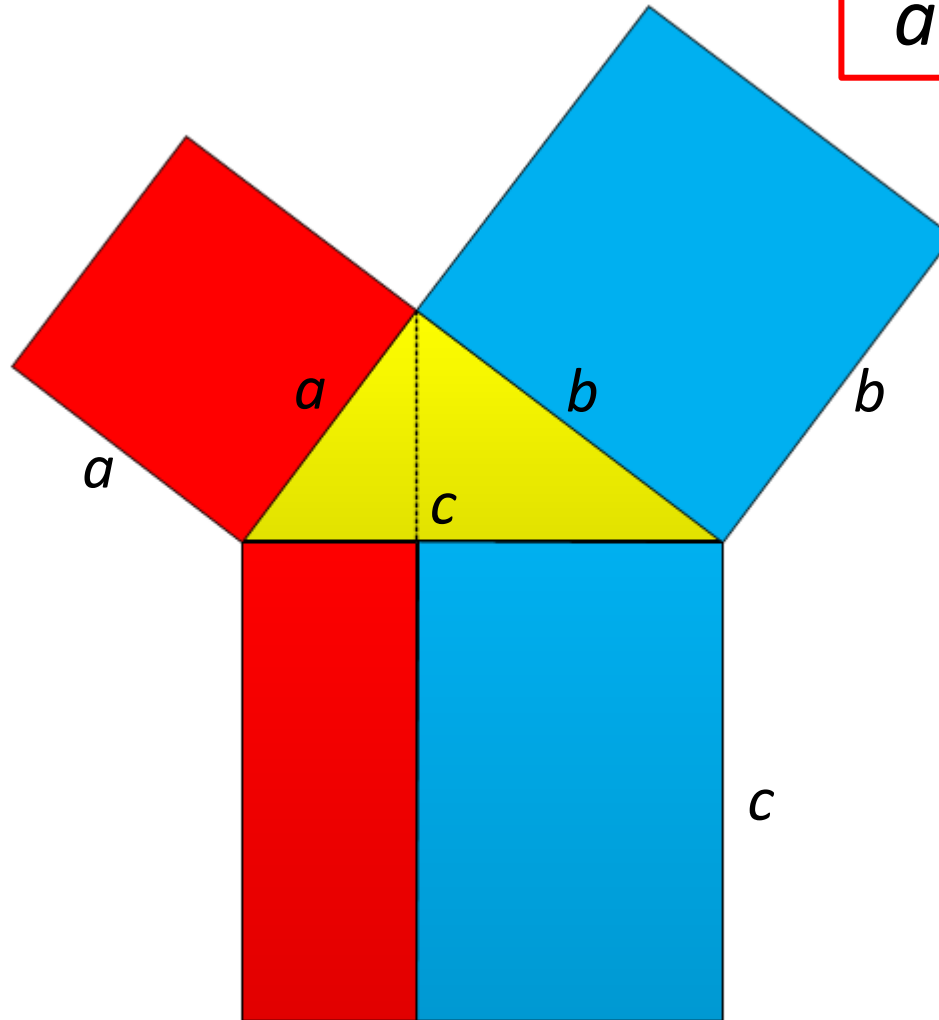


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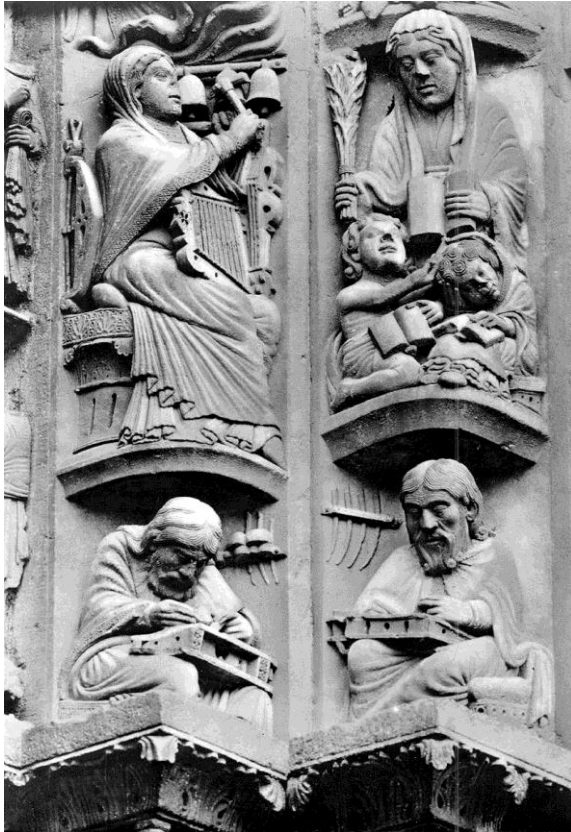
Pythagoras' Theorem

$$a^2 + b^2 = c^2$$

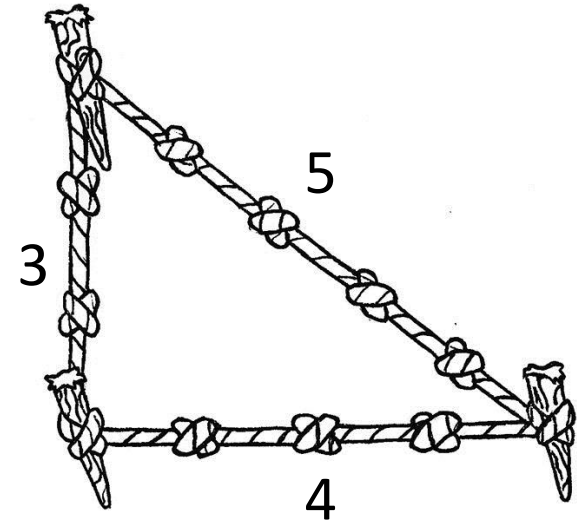


Pythagoras' Theorem

$$3^2 + 4^2 = 5^2$$

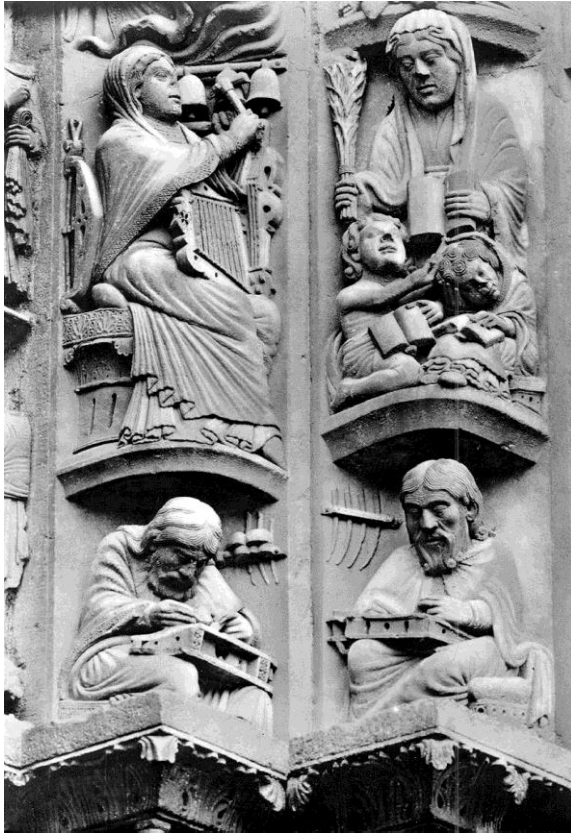


Pythagoras at Chartres Cathedral



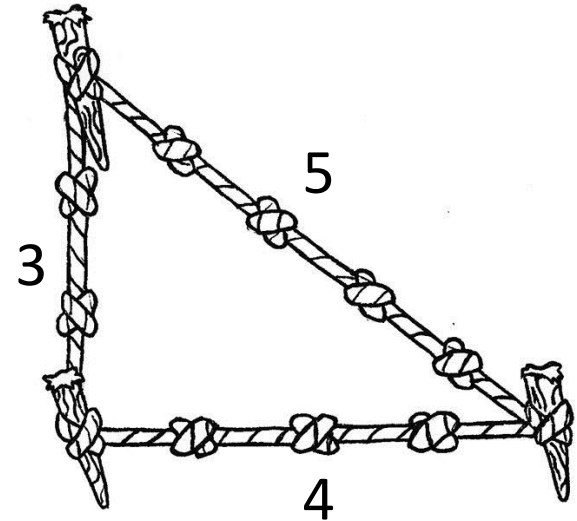
Pythagoras' Theorem

Music

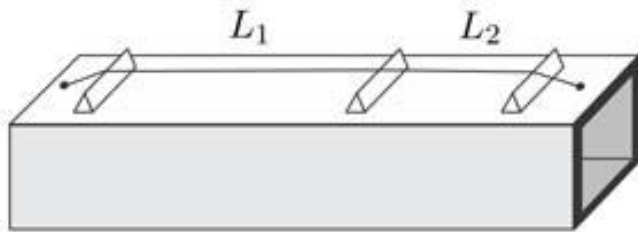


Pythagoras at Chartres Cathedral

$$3^2 + 4^2 = 5^2$$



Pythagoras and Music



Can the ratios of small numbers give us a perfect musical system?

$L_1 = 1/2$, $L_2 = 1/2$: unison;

$L_1 = 1/3$, $L_2 = 2/3$: octave;

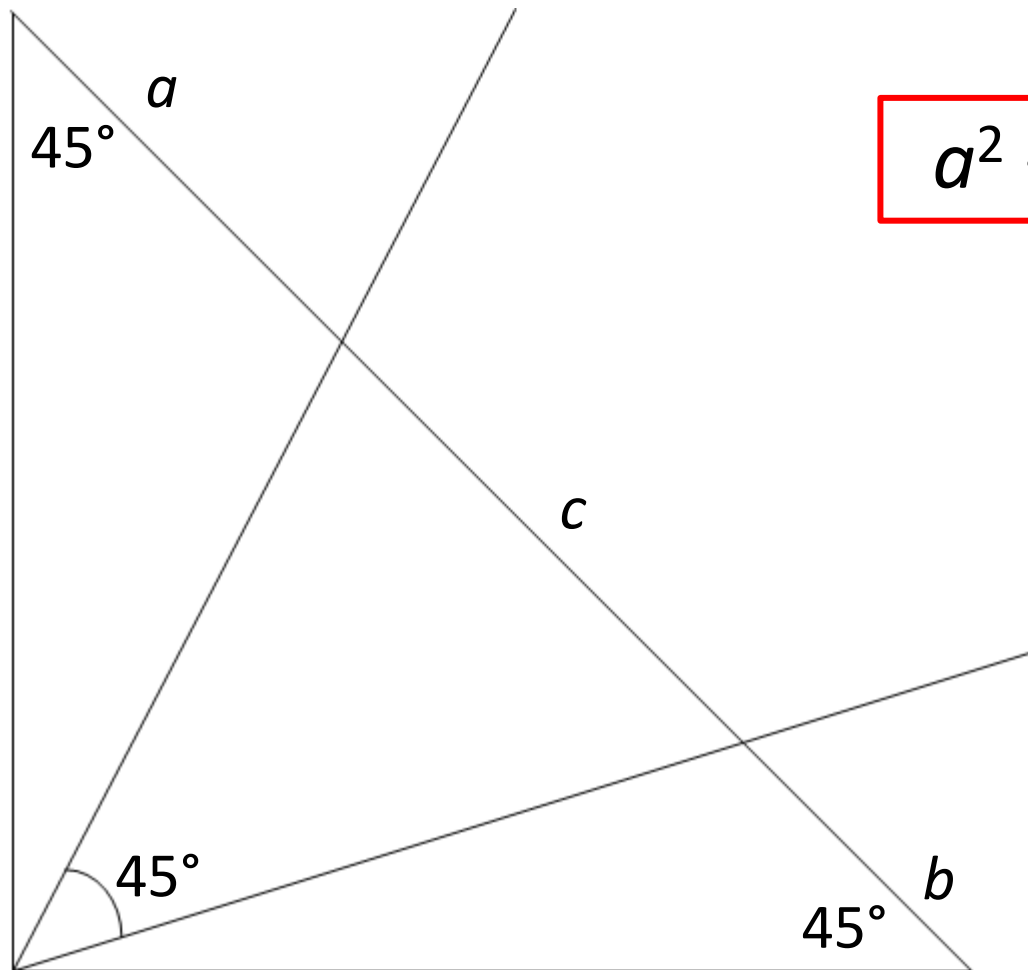
$L_1 = 3/5$, $L_2 = 2/5$: perfect fifth;

$L_1 = 4/7$, $L_2 = 3/7$: perfect fourth

Two intervals that add up to an octave are each other's inversions:
e.g. $3/2 \times 4/3 = 2$, so a fourth is the inversion of the fifth, etc.

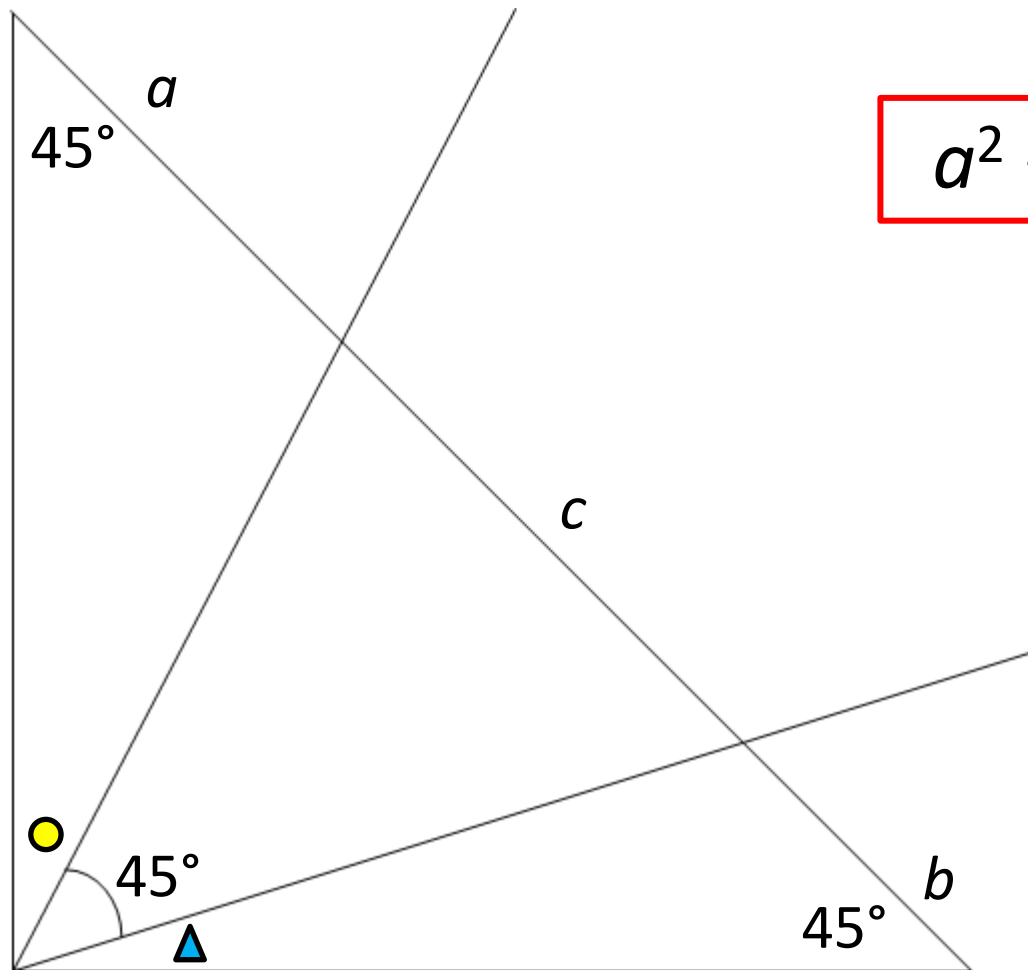


Pythagoras' Theorem



$$a^2 + b^2 = c^2$$

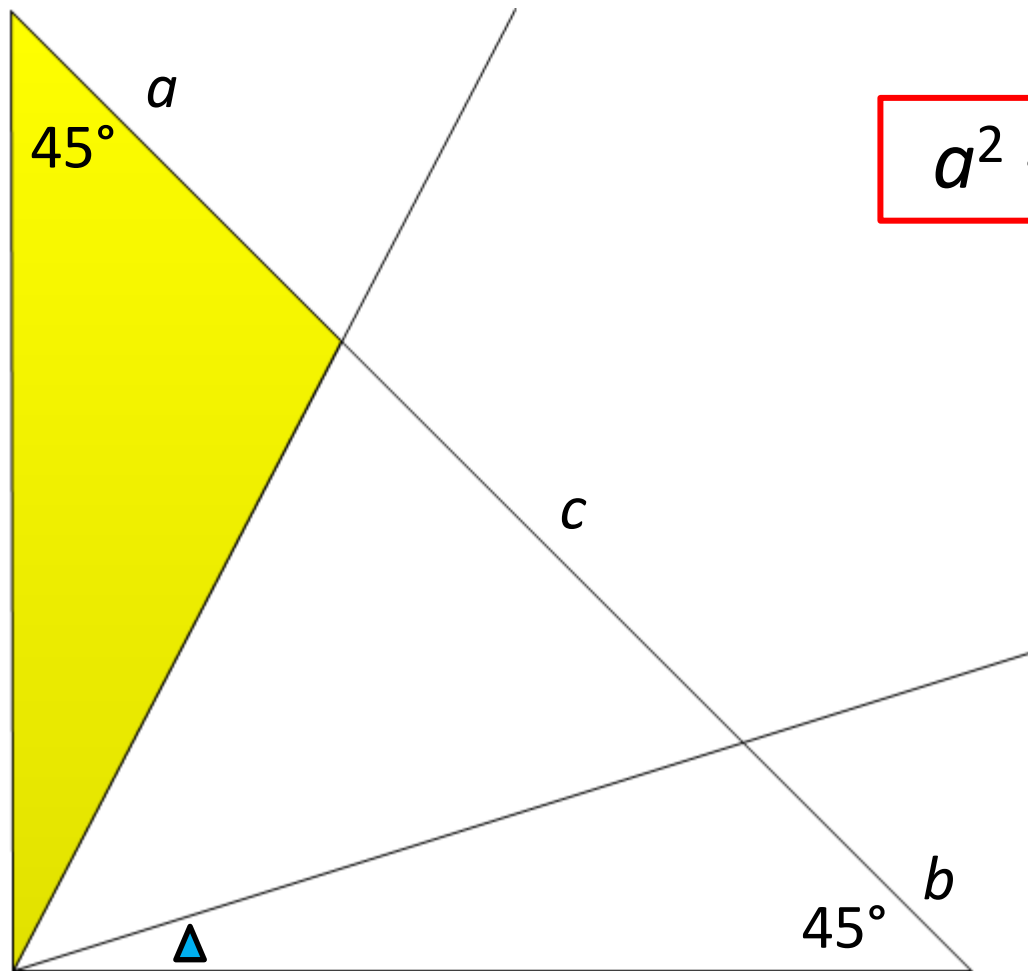
Pythagoras' Theorem



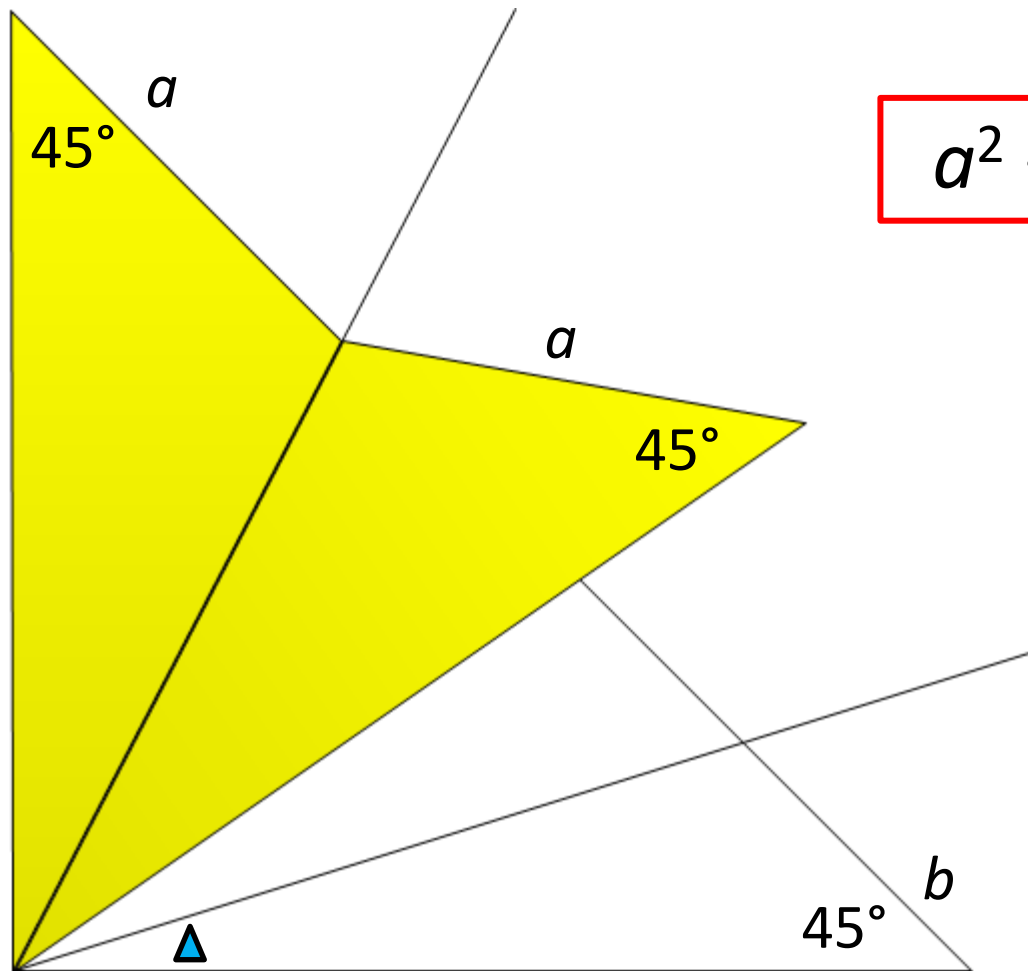
$$a^2 + b^2 = c^2$$



Pythagoras' Theorem

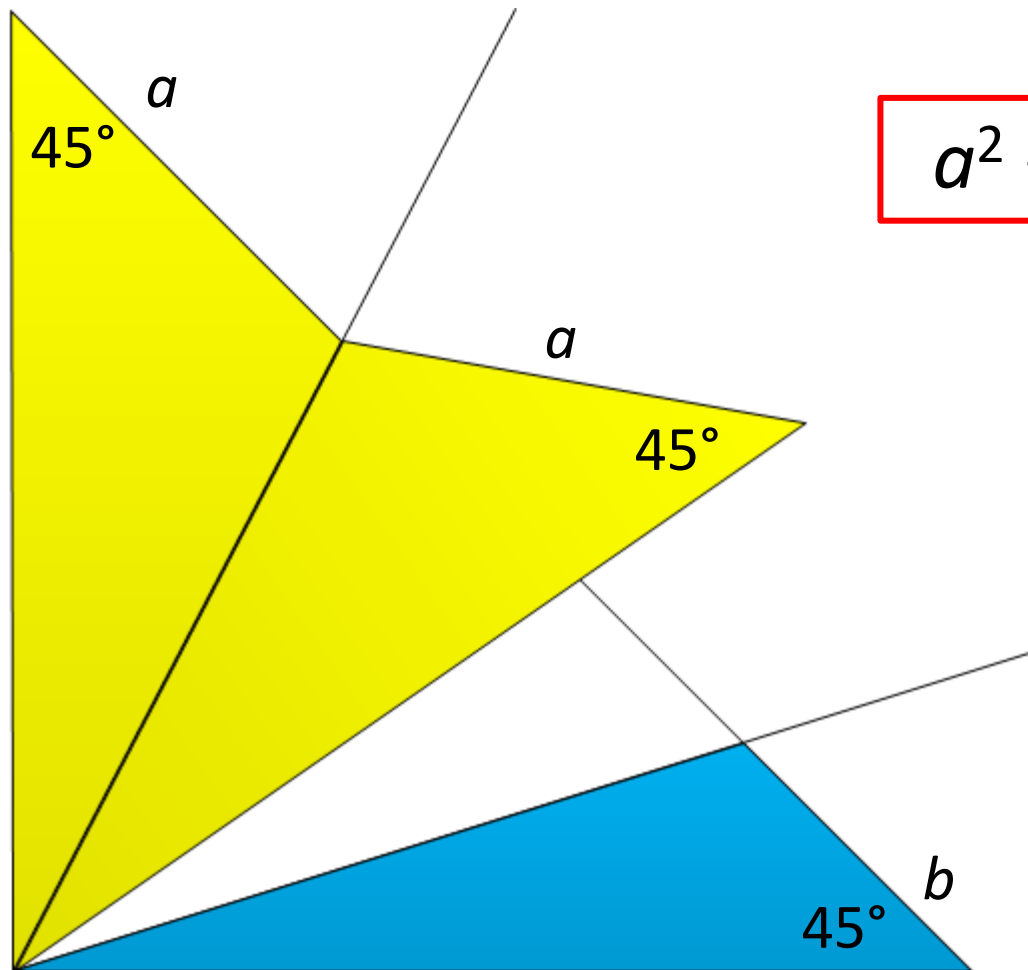


Pythagoras' Theorem



$$a^2 + b^2 = c^2$$

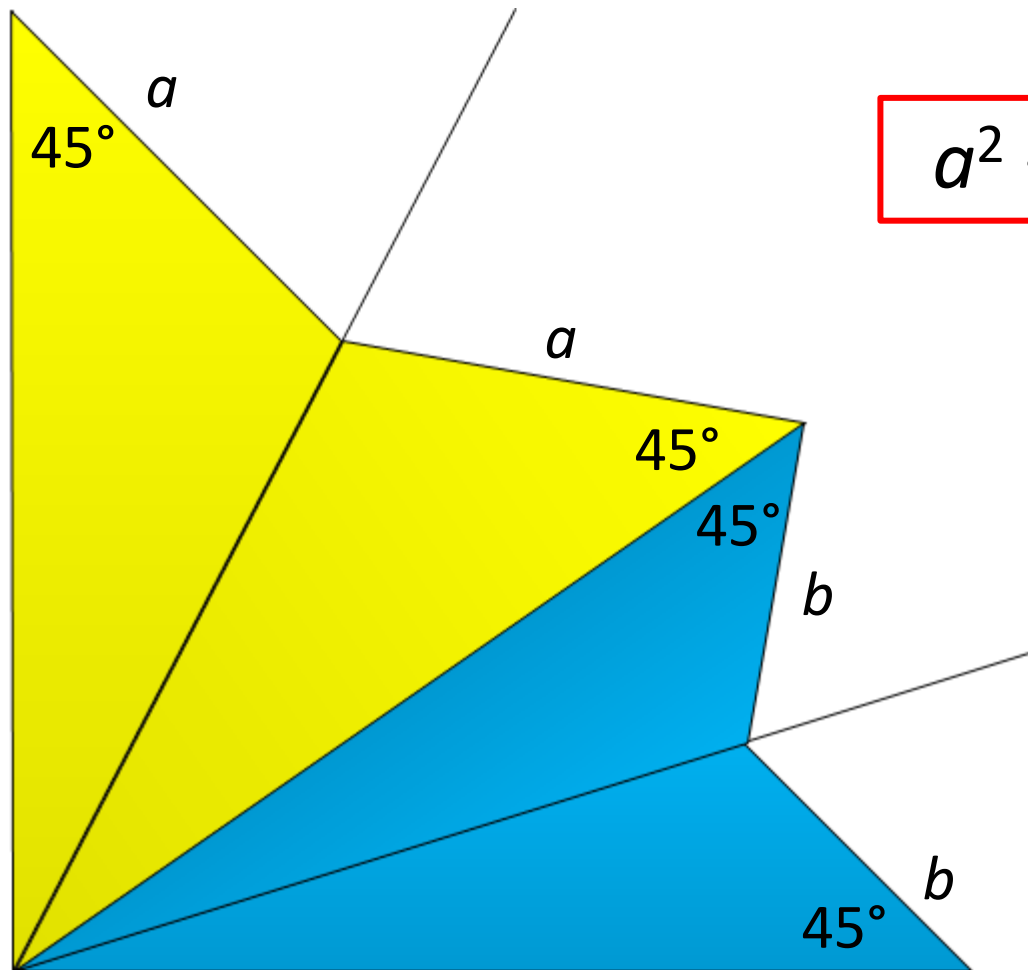
Pythagoras' Theorem



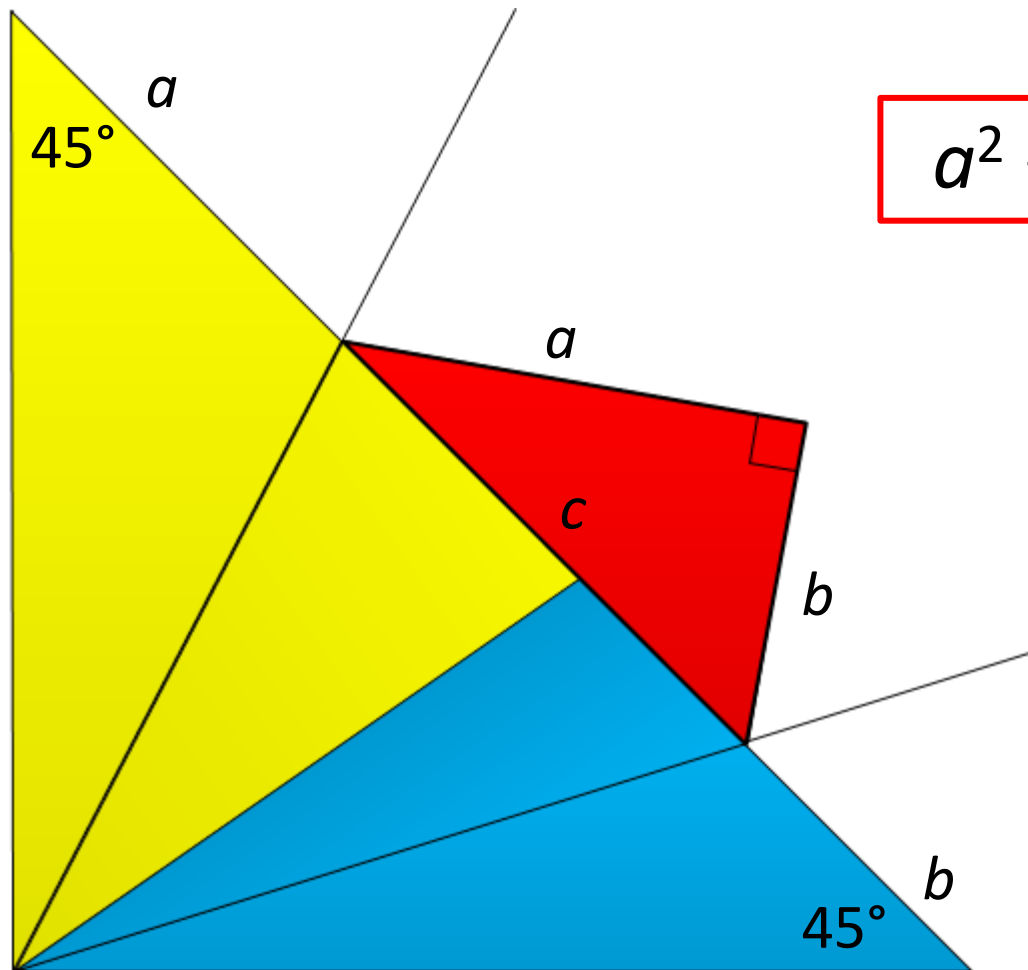
$$a^2 + b^2 = c^2$$



Pythagoras' Theorem

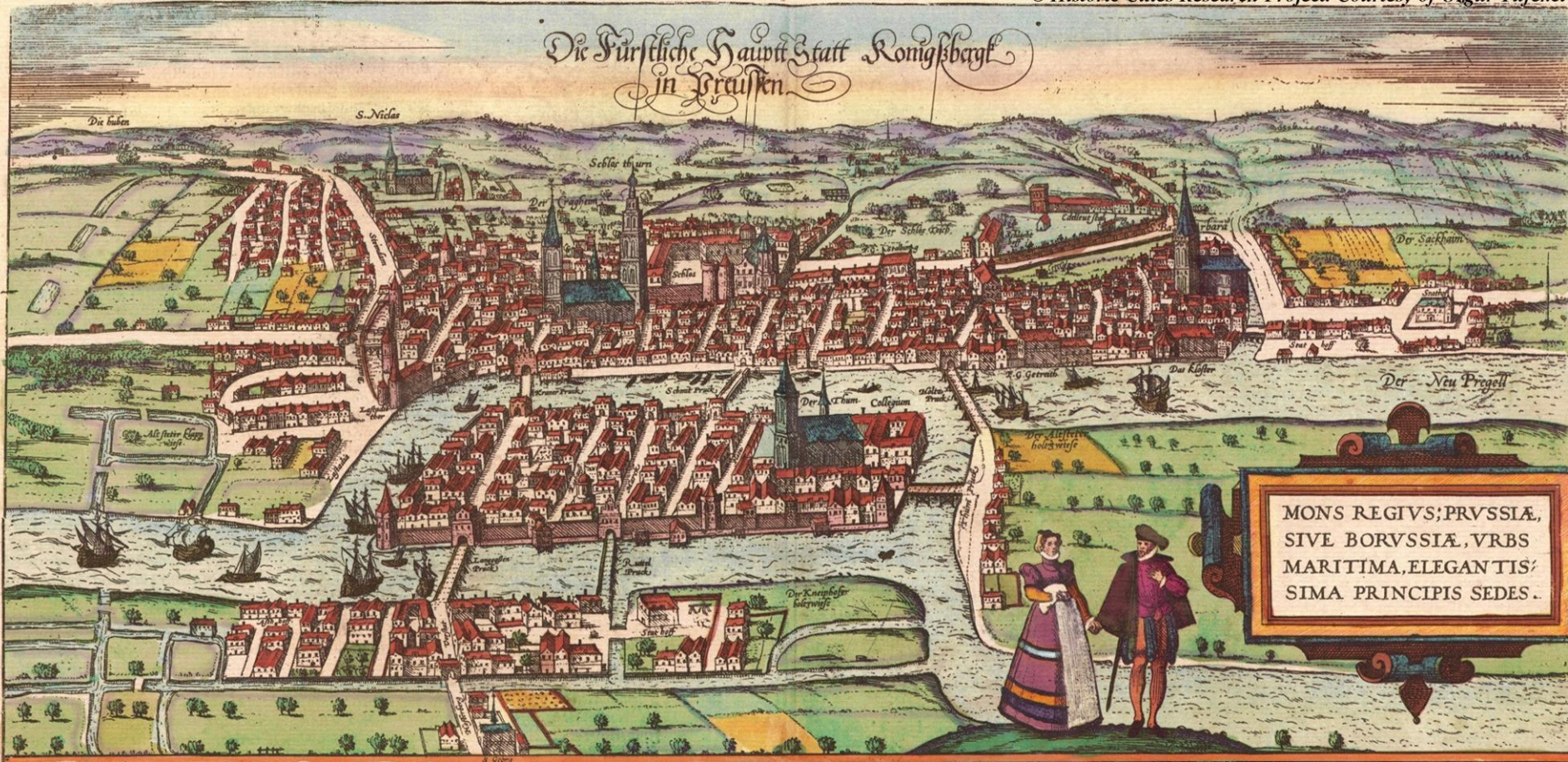


Pythagoras' Theorem

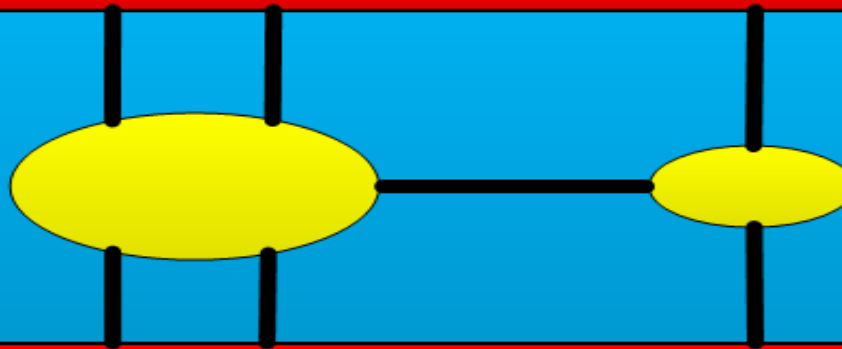


Seven Bridges of Königsberg (± 1730)

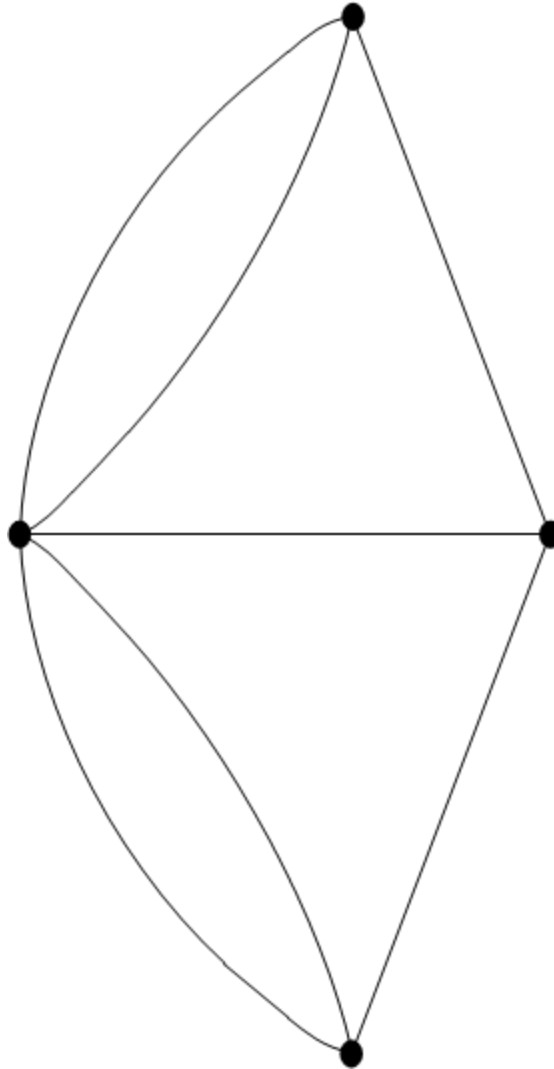
© Historic Cities Research Project. Courtesy of Özgür Tufekci



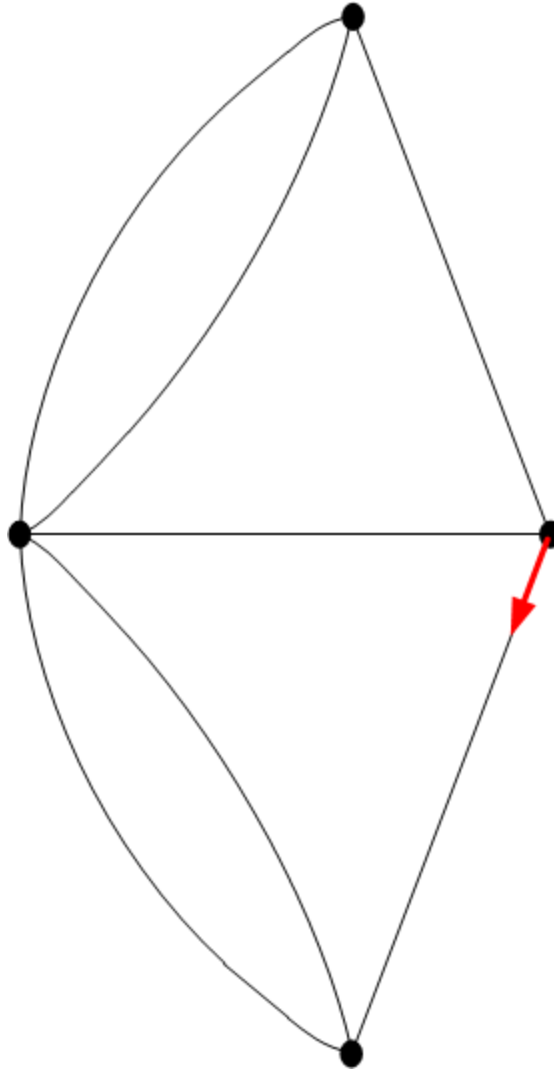
Seven Bridges of Königsberg (± 1730)



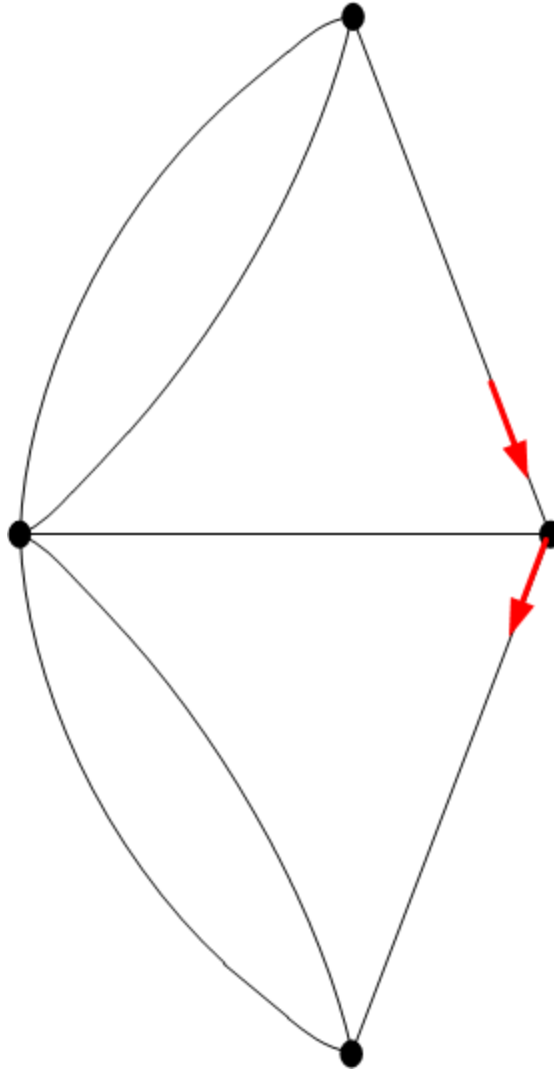
Leonard Euler (1707-1783)



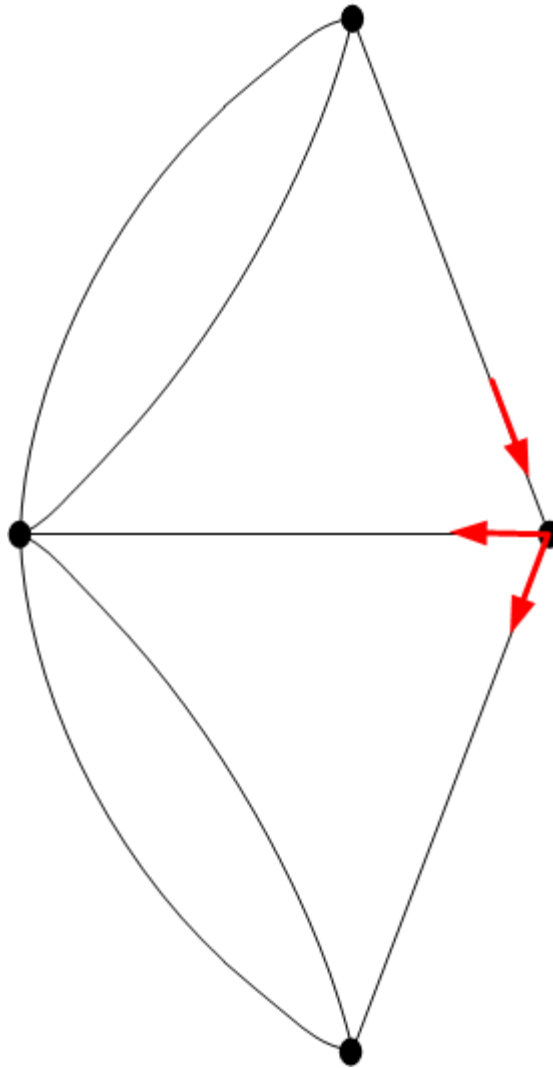
Leonard Euler (1707-1783)



Leonard Euler (1707-1783)

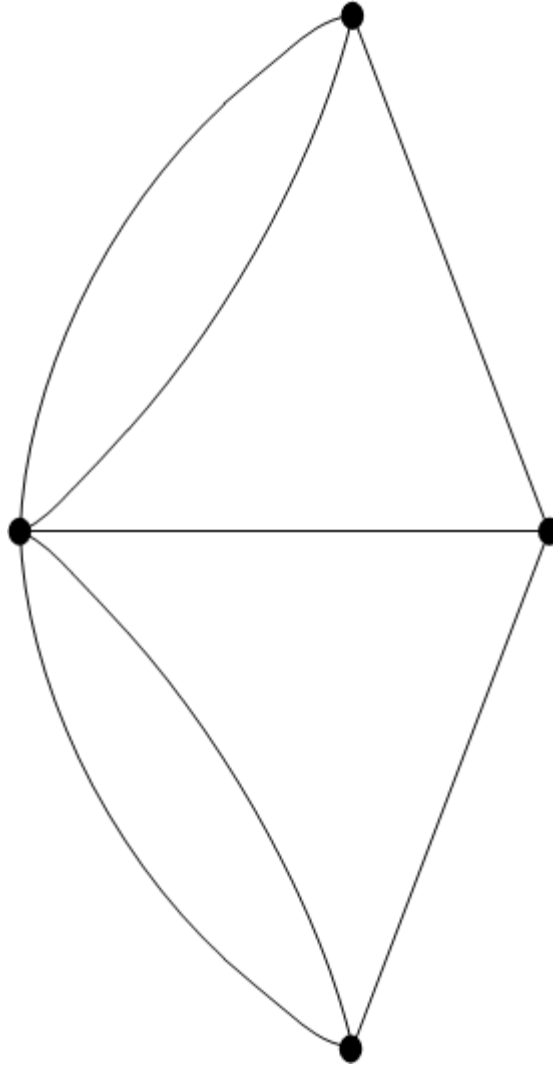


Leonard Euler (1707-1783)

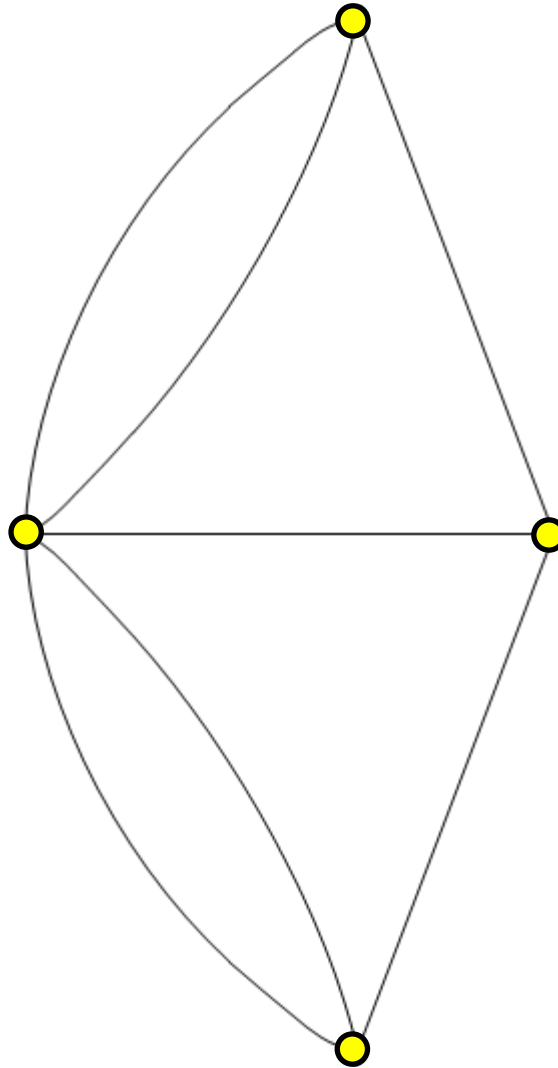


Leonard Euler (1707-1783)

$$V - E + F = 2$$



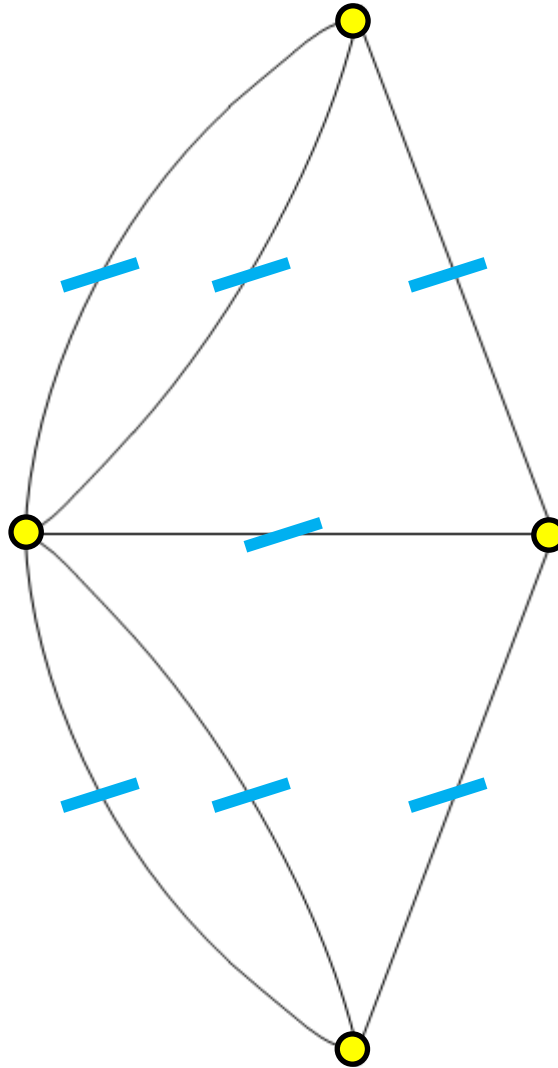
Leonard Euler (1707-1783)



$$V - E + F = 2$$

4

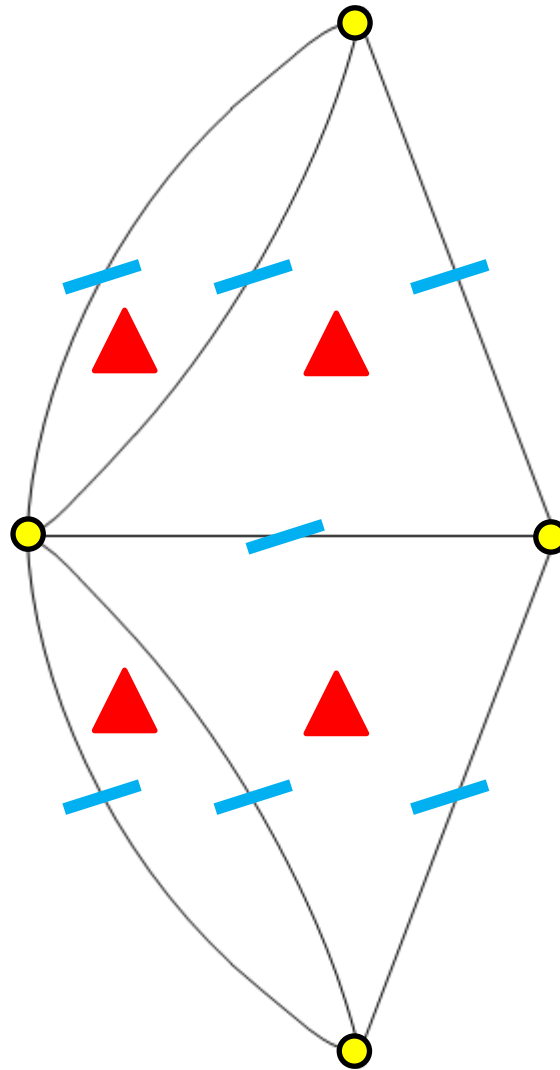
Leonard Euler (1707-1783)



$$V - E + F = 2$$

$$4 - 7$$

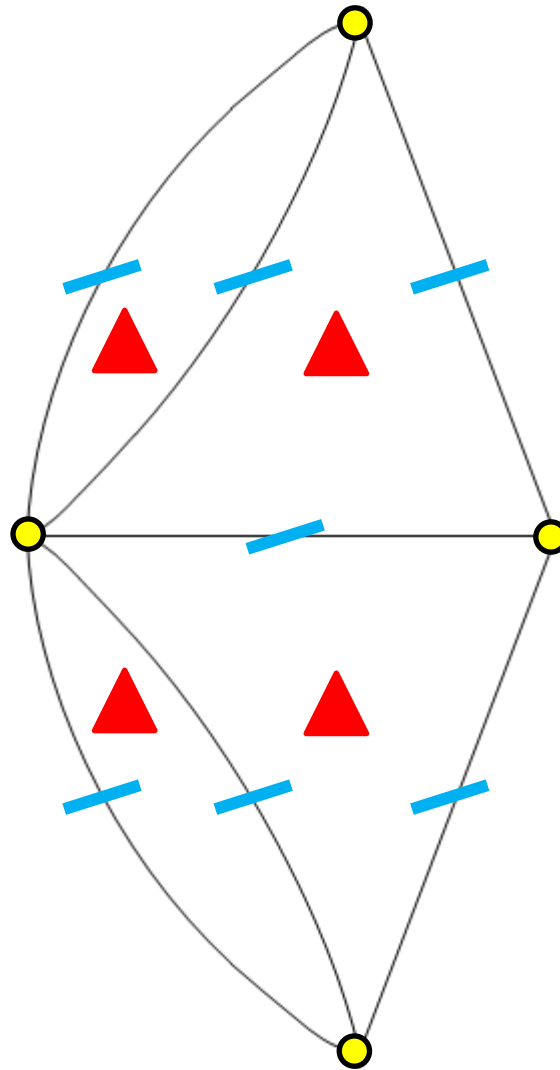
Leonard Euler (1707-1783)



$$V - E + F = 2$$

$$4 - 7 + 5$$

Leonard Euler (1707-1783)

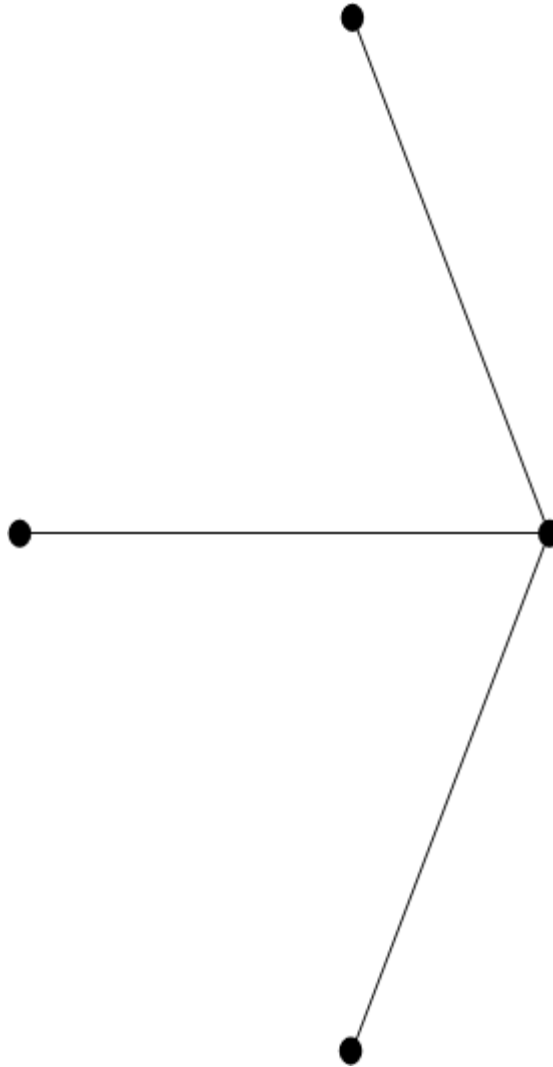


$$V - E + F = 2$$

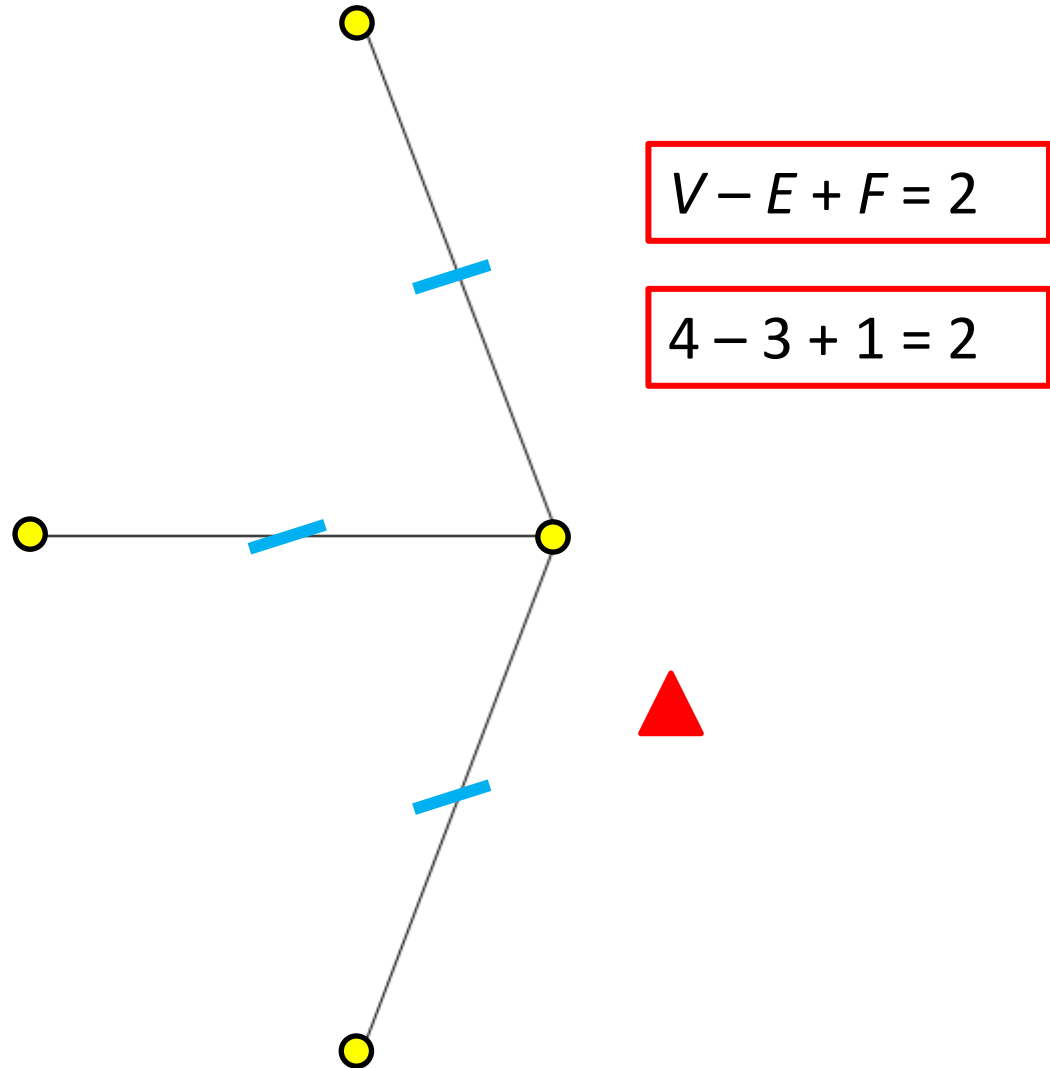
$$4 - 7 + 5 = 2$$

Leonard Euler (1707-1783)

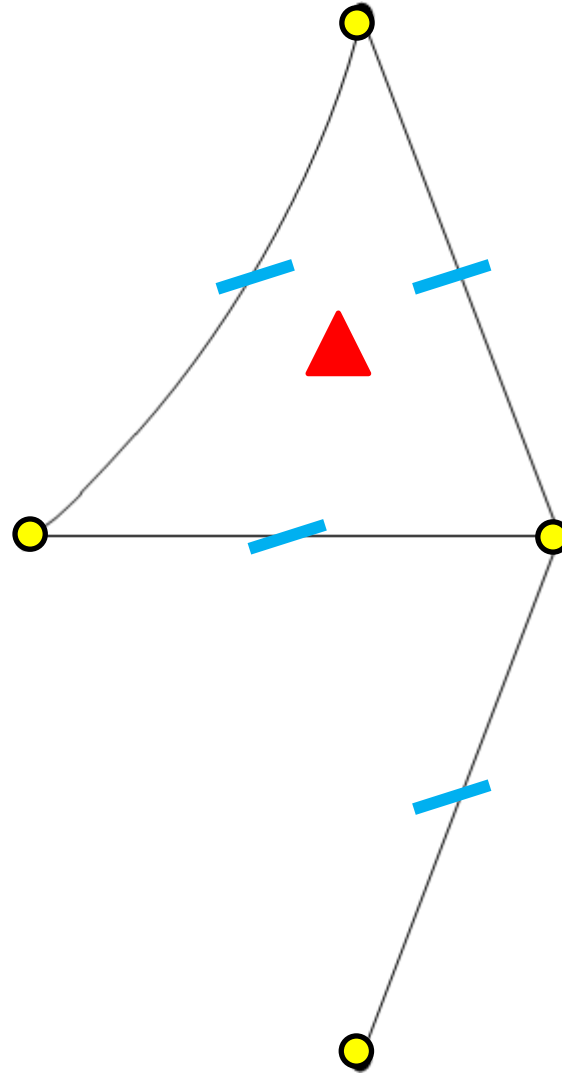
$$V - E + F = 2$$



Leonard Euler (1707-1783)



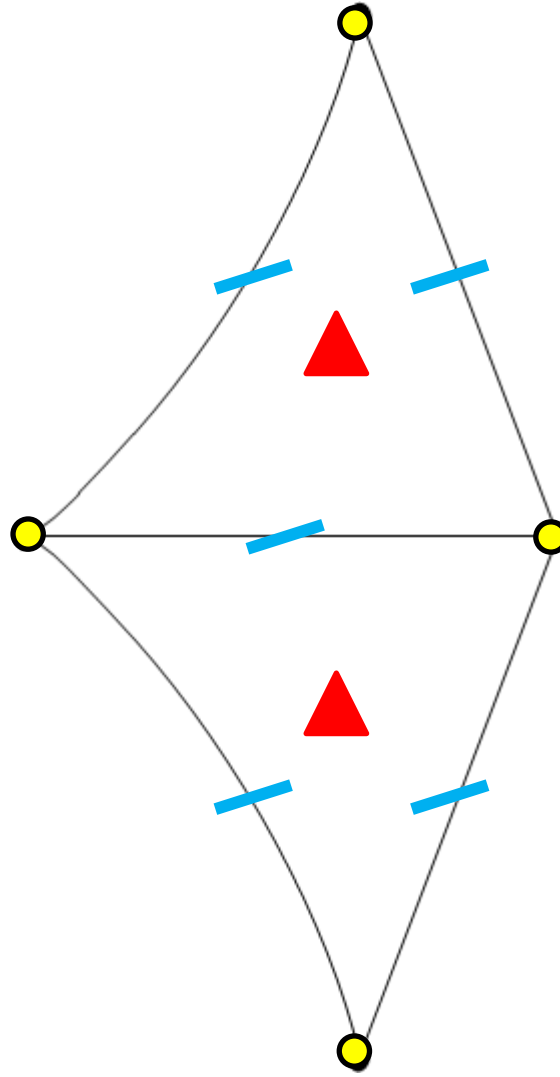
Leonard Euler (1707-1783)



$$V - E + F = 2$$

$$4 - 4 + 2 = 2$$

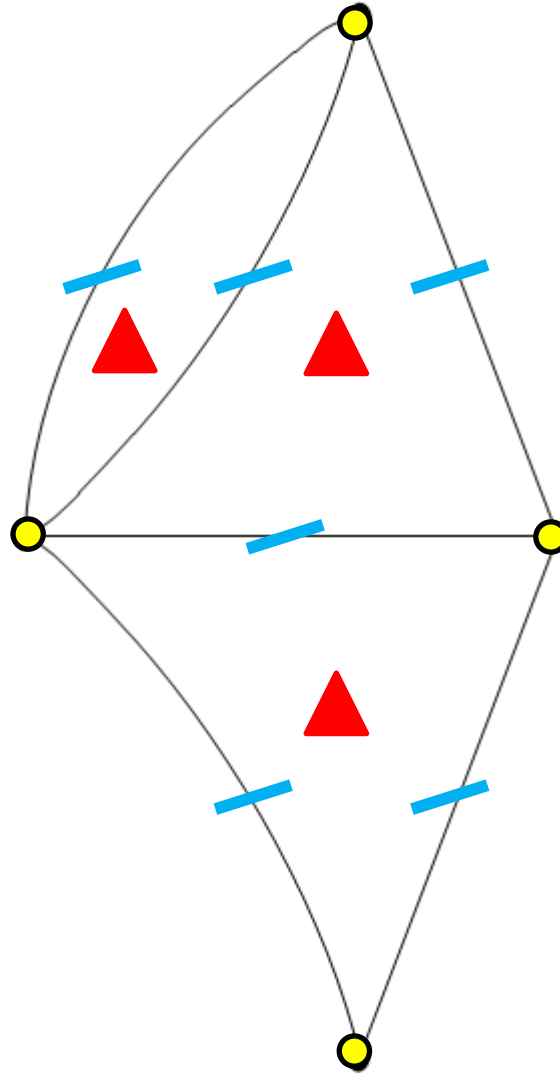
Leonard Euler (1707-1783)



$$V - E + F = 2$$

$$4 - 5 + 3 = 2$$

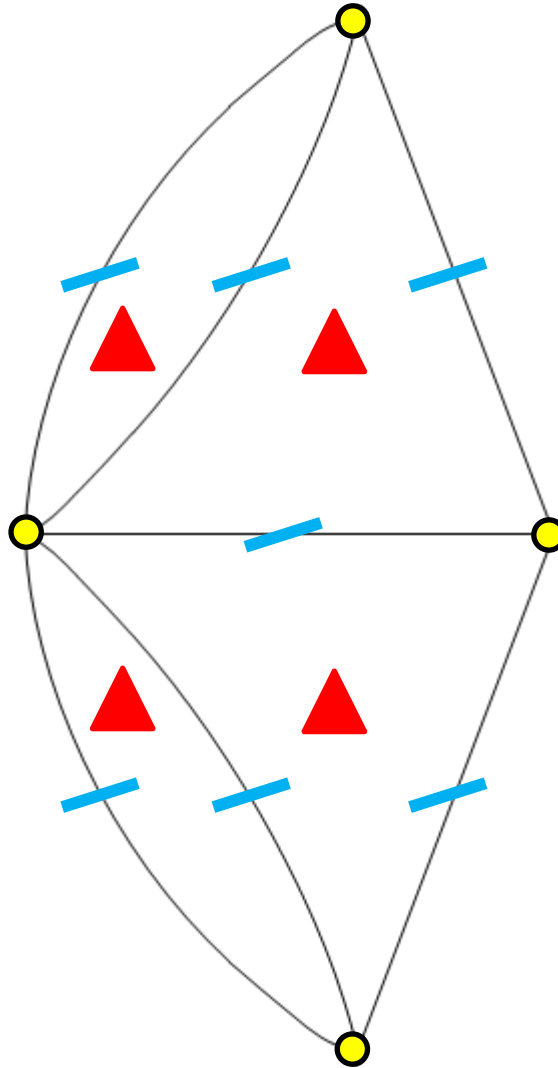
Leonard Euler (1707-1783)



$$V - E + F = 2$$

$$4 - 6 + 4 = 2$$

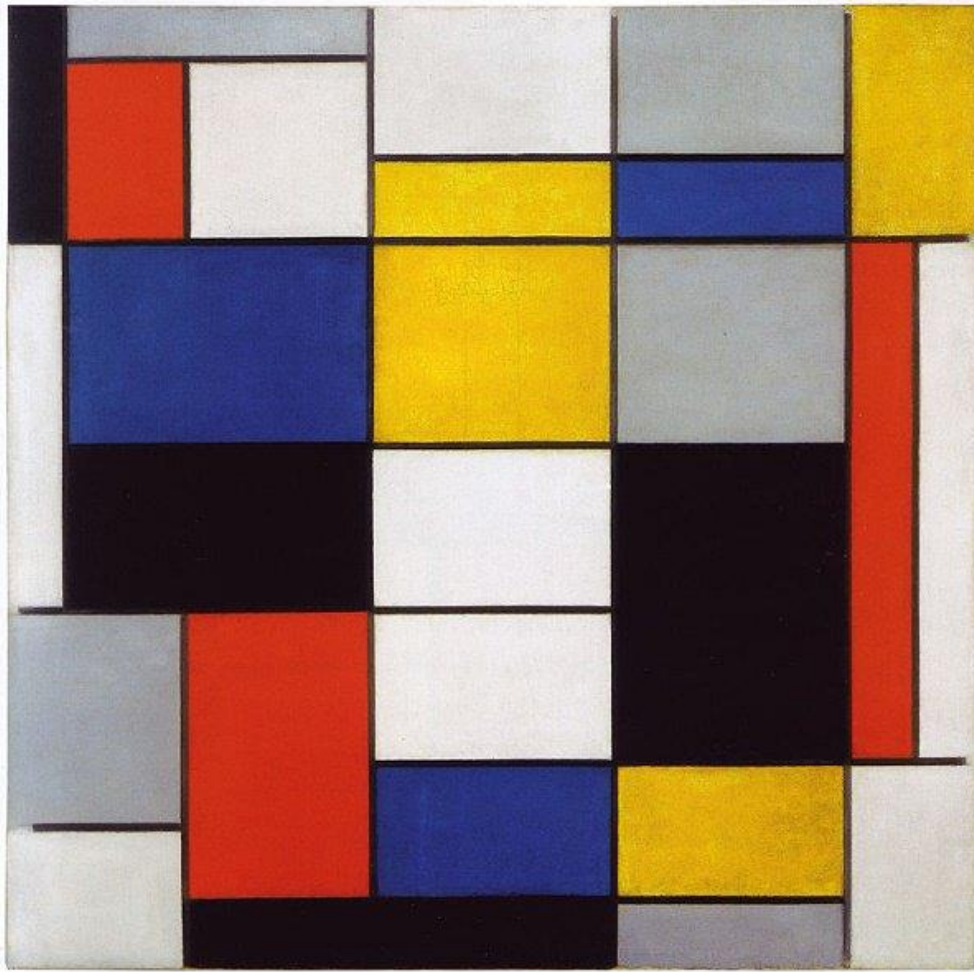
Leonard Euler (1707-1783)



$$V - E + F = 2$$

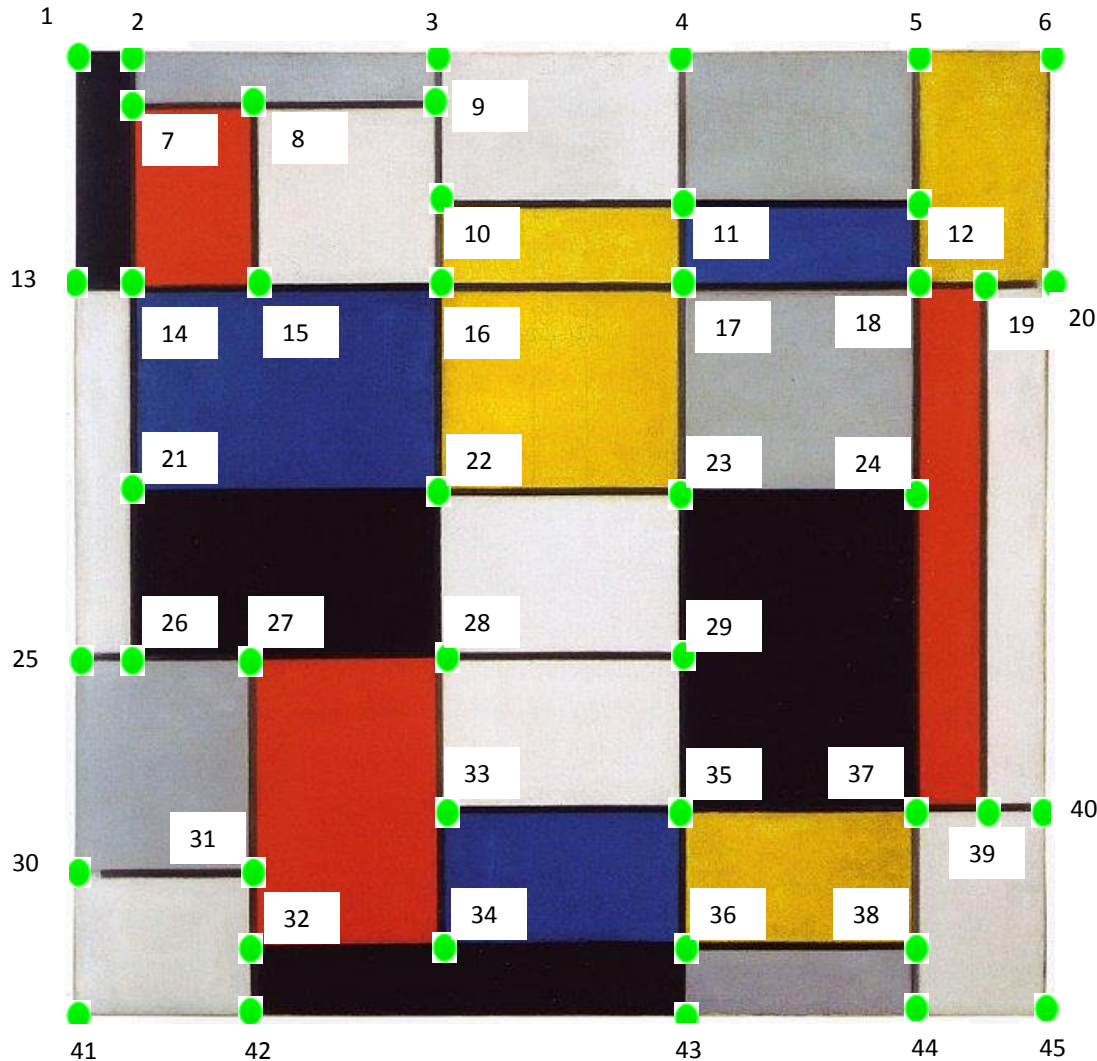
$$4 - 7 + 5 = 2$$

Euler and Mondriaan



$$V - E + F = 2$$

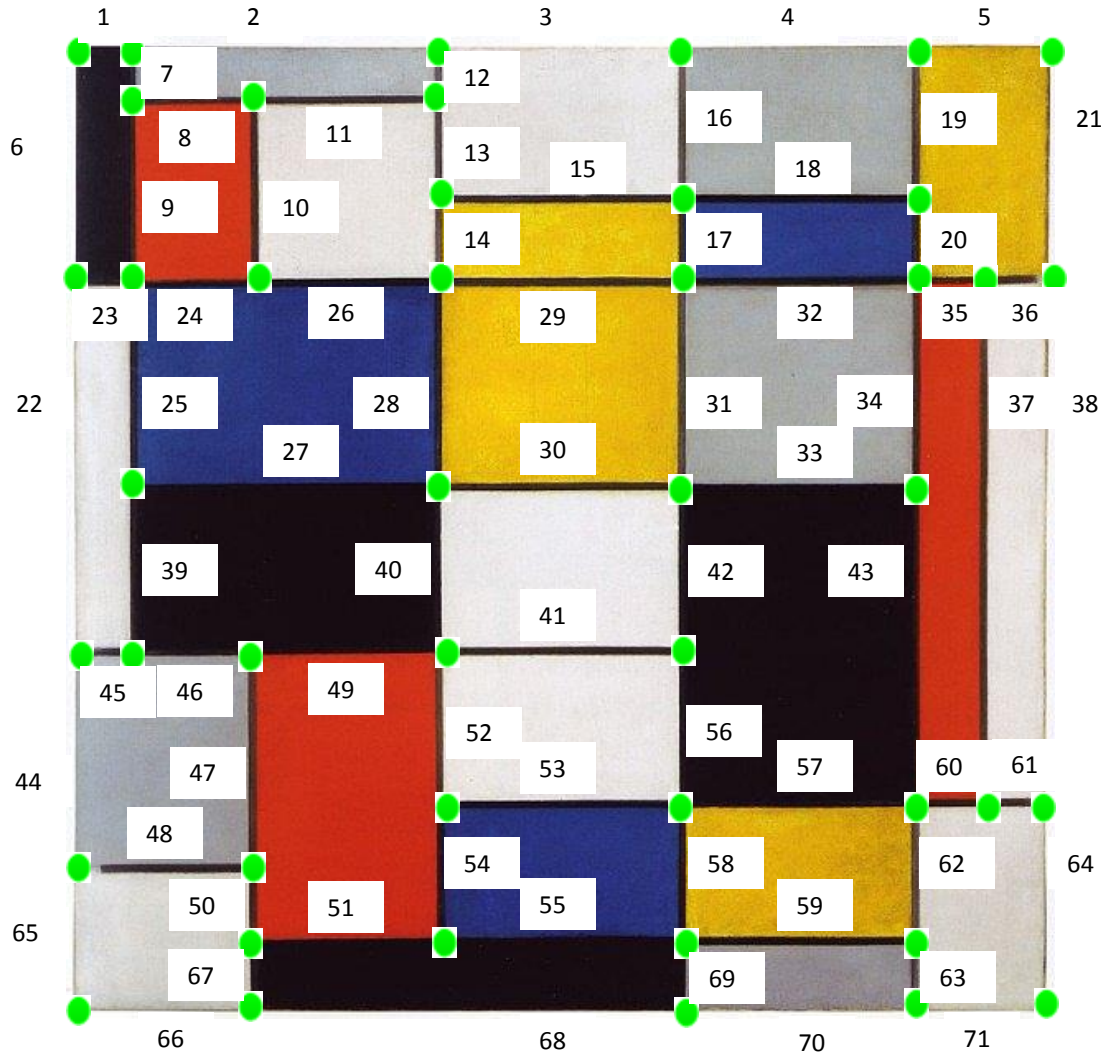
Euler and Mondriaan



$$V - E + F = 2$$

45

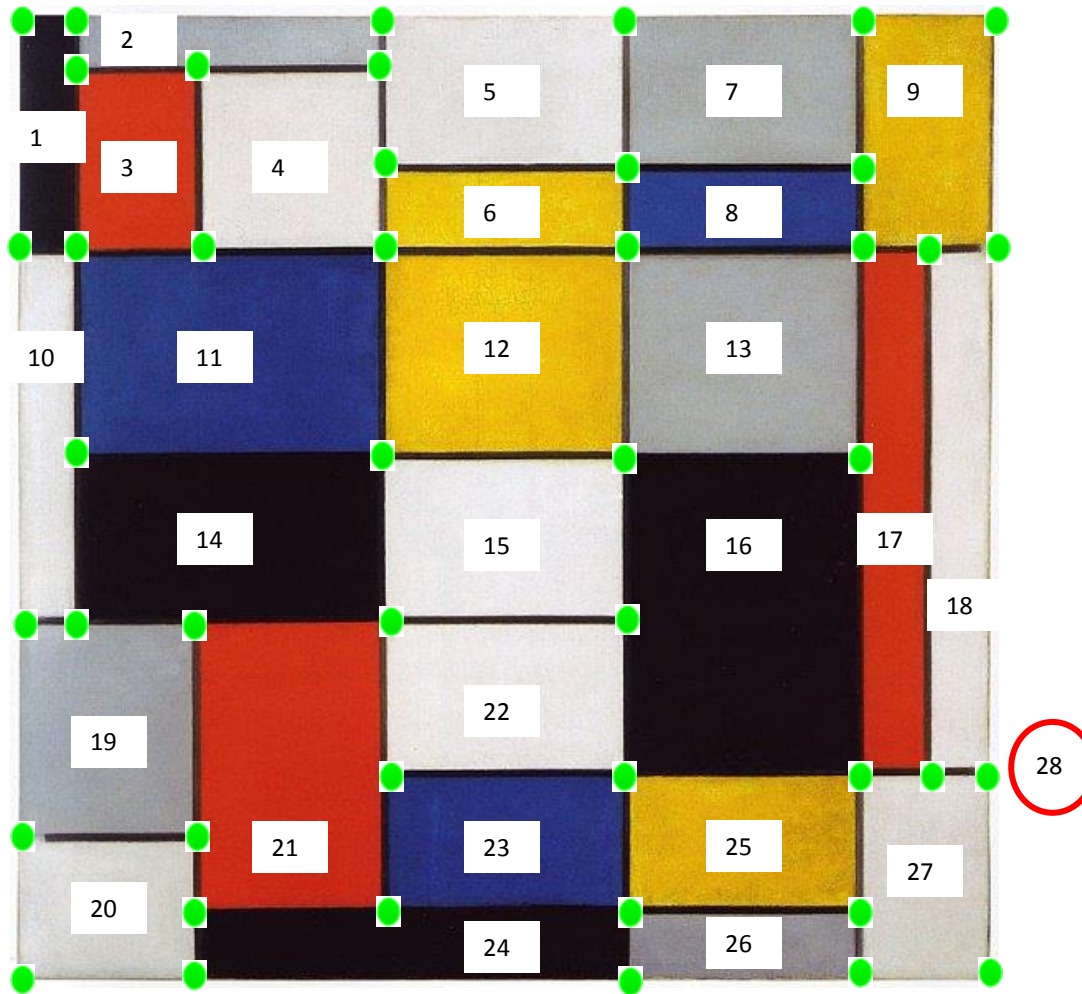
Euler and Mondriaan



$$V - E + F = 2$$

$$45 - 71$$

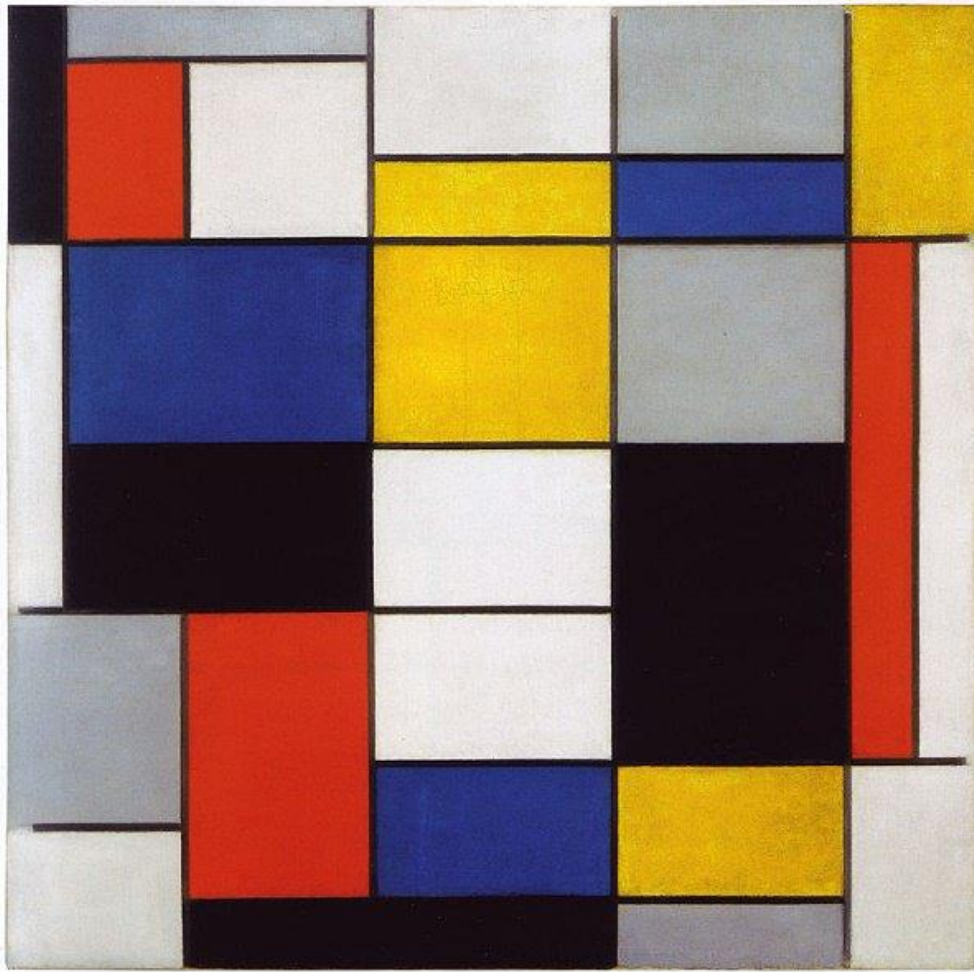
Euler and Mondriaan



$$V - E + F = 2$$

$$45 - 71 + 28$$

Euler and Mondriaan



$$V - E + F = 2$$

$$45 - 71 + 28 = 2$$

PLATONIC SOLIDS

TETRAHEDRON

'FOUR SIDED'



△ FIRE

4 FACES
4 POINTS
6 EDGES

OCTAHEDRON

'EIGHT SIDED'



△ AIR

8 FACES
6 POINTS
12 EDGES

HEXAHEDRON

'SIX SIDED'



▽ EARTH

6 FACES
8 POINTS
12 EDGES

ICOSAHEDRON

'TWENTY SIDED'



▽ WATER

20 FACES
12 POINTS
30 EDGES

DODECAHEDRON

'TWELVE SIDED'



☼ AETHER

12 FACES
20 POINTS
30 EDGES

$$V - E + F = 2$$

$$4 - 6 + 4 = 2$$

$$V - E + F = 2$$

$$6 - 12 + 8 = 2$$

$$V - E + F = 2$$

$$8 - 12 + 6 = 2$$

$$V - E + F = 2$$

$$12 - 30 + 20 = 2$$

$$V - E + F = 2$$

$$20 - 30 + 12 = 2$$

Beautiful Numbers



Maastricht University

Department of Data Science and Knowledge Engineering



f.thuijsman@maastrichtuniversity.nl

TAOP - I Am A Painter, Maastricht, November 1, 2017

Beautiful Numbers

$$\pi = 3.14159\dots$$



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

$e = 2.71828\dots$



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

$$e = 2.71828\dots \quad e = 1 + \frac{1}{1} + \frac{1}{2*1} + \frac{1}{3*2*1} + \frac{1}{4*3*2*1} + \dots$$



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

$e = 2.71828\dots$ $e = 1 + \frac{1}{1} + \frac{1}{2*1} + \frac{1}{3*2*1} + \frac{1}{4*3*2*1} + \dots$

$i = ?$



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

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$i = ?$ $i^2 = -1$, i is an imaginary number



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

$e = 2.71828\dots$ $e = 1 + \frac{1}{1} + \frac{1}{2*1} + \frac{1}{3*2*1} + \frac{1}{4*3*2*1} + \dots$

$i = ?$ $i^2 = -1$, i is an imaginary number

$$e^{\pi i} + 1 = 0$$



Beautiful Numbers

$\pi = 3.14159\dots$ half circumference of circle with radius 1

$e = 2.71828\dots$ $e = 1 + \frac{1}{1} + \frac{1}{2*1} + \frac{1}{3*2*1} + \frac{1}{4*3*2*1} + \dots$

$i = ?$ $i^2 = -1$, i is an imaginary number

$$e^{\pi i} + 1 = 0$$

THANKS



Enjoy the Abstract in Art and Beyond!

$$e^{\pi i} + 1 = 0$$

THANKS



Enjoy the Abstract in Art and Beyond!

$$e^{\pi i} + 1 = 0$$

THANKS

